



# **Design and Implementation of Efficient Carry Select Adder in QCA**

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**ABSTRACT:** In this brief, the logic operations involved in conventional carry select adder (CSLA) and binary to excess-1 converter (BEC)-based CSLA are analyzed to study the data dependence and to identify redundant logic operations. We have eliminated all the redundant logic operations present in the conventional CSLA and proposed a new logic formulation for CSLA. In the proposed scheme, the carry select (CS) operation is scheduled before the calculation of final-sum, which is different from the conventional approach. Bit patterns of two anticipating carry words (corresponding to  $c_{in} = 0$  and 1) and fixed  $c_{in}$  bits are used for logic optimization of CS and generation units. An efficient CSLA design is obtained using optimized logic units. The proposed CSLA design involves significantly less area and delay than the recently proposed BEC-based CSLA. Due to the small carry-output delay, the proposed CSLA design is a good candidate for square-root (SQRT) CSLA. Here we are implementing one new carry select adder by using QCA (Quantum-Dot Cellular Automata) in efficient way compared to existing methodologies. As transistors decrease in size more and more of them can be accommodated in a single die, thus increasing chip computational capabilities. However, transistors cannot get much smaller than their current size. The quantum-dot cellular automata (QCA) approach represents one of the possible solutions in overcoming this physical limit, even though the design of logic modules in QCA is not always straightforward. In this brief, we propose a new adder that outperforms all state-of-the-art competitors and achieves the best area-delay tradeoff.

**KEYWORDS:** Aging effects, Aging indicators, Adaptive hold logic (AHL), Bias Temperature Instability, reliable multiplier, variable latency, fixed latency.

## **I. INTRODUCTION**

Quantum-dot cellular automata (QCA) are an attractive emerging technology suitable for the development of ultra-dense low-power high-performance digital circuits. Quantum-dot cellular automata (QCA) which employs array of coupled quantum dots to implement Boolean logic function. The advantage of QCA lies in the extremely high packing densities possible due to the small size of the dots, the simplified interconnection, and the extremely low power delay product. A basic QCA cell consists of four quantum dots in a square array coupled by tunnel barriers. Electrons are able to tunnel between the dots, but cannot leave the cell. If two excess electrons are placed in the cell, Coulomb repulsion will force the electrons to dots on opposite corners. There are thus two energetically equivalent ground state polarizations can be labeled logic "0" and "1". The basic building blocks of the QCA architecture are AND, OR and NOT. By using the Majority gate we can reduce the amount of delay. i.e by calculating the propagation and generational carries. Design of area- and power-efficient high-speed data path logic systems are one of the most substantial areas of research in VLSI system design. Concatenating the N full adders forms N bit Ripple carry adder. In this carry out of previous full adder becomes the input carry for the next full adder. It calculates sum and carry according to the following equations. As carry ripples from one full adder to the other, it traverses longest critical path and exhibits worst-case delay.

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$$S_i = A_i \oplus B_i \oplus C_i$$

$$C_{i+1} = A_i B_i + (A_i + B_i) C_i$$

where  $i = 0, 1, \dots, n-1$

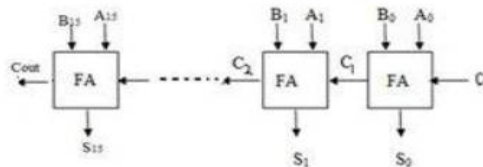


FIG:1 Ripple carry adder

RCA is the slowest in all adders ( $O(n)$  time) but it is very compact in size ( $O(n)$  area). If the ripple carry adder is implemented by concatenating  $N$  full adders, the delay of such an adder is  $2N$  gate delays from  $C_{in}$  to  $C_{out}$ . The delay of adder increases linearly with increase in number of bits. Block diagram of RCA is shown in figure 1. In digital adders, the speed of addition is limited by the time required to propagate a carry through the adder. The sum for each bit position in an elementary adder is generated sequentially only after the previous bit position has been summed and a carry propagated into the next position. The CSLA is used in many computational systems to alleviate the problem of carry propagation delay by independently generating multiple carries and then select a carry to generate the sum [1]. However, the CSLA is not area efficient because it uses multiple pairs of Ripple Carry Adders (RCA) to generate partial sum and carry by considering carry input  $C_{in}=0$  and  $C_{in}=1$  then the final sum and carry are selected by the multiplexers (mux). The basic idea of this work is to use Binary to Excess-1 Converter (BEC) instead of RCA with  $C_{in}=1$  in the regular CSLA to achieve lower area and power consumption [2]–[4]. The main advantage of this BEC logic comes from the lesser number of logic gates than the  $n$ -bit Full Adder (FA) structure.

## II. LITERATURE SURVEY

Proposed a square-root (SQRT)-CSLA to implement large bit-width adders with less delay. In a SQRT CSLA, with increasing size are connected in a cascading structure. The main objective of SQRT-CSLA design is to provide a parallel path for carry propagation that helps to reduce the overall adder delay. Ram kumar and Kittur [6] suggested a binary to BEC-based CSLA. The BEC-based CSLA involves less logic resources than the conventional CSLA, but it has marginally higher delay. A CSLA based on common Boolean logic (CBL) is also proposed in [7] and [8]. The CBL-based CSLA of [7] involves significantly less logic resource than the conventional CSLA but it has longer CPD, which is almost equal to that of the RCA. To overcome this problem, a SQRT-CSLA based on CBL was proposed in [8]. However, the CBL-based SQRTCSLA design of [8] requires more logic resource and delay than the BEC-based SQRT-CSLA of [6]. We observe that logic optimization largely depends on availability of redundant operations in the formulation, whereas adder delay mainly depends on data dependence. In the existing designs, logic is optimized without giving any consideration to the data dependence. In this brief, we made an analysis on logic operations involved in conventional and BEC-based CSLAs to study the data dependence and to identify redundant logic operations. Based on this analysis, we have proposed a logic formulation for the CSLA. The main contribution in this brief is logic formulation based on data dependence and optimized carry generator (CG) and CS design. Based on the proposed logic formulation, we have derived an efficient logic.

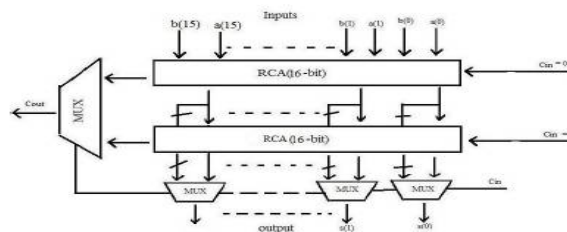


Fig:2 conventional CSLA

### III. EXISTING METHODOLOGIES

The CSLA has two units: 1) the *sum* and *carry* generator unit (SCG) and 2) the *sum* and *carry* selection unit [9]. The SCG unit consumes most of the logic resources of CSLA and significantly contributes to the critical path. Different logic designs have been suggested for efficient implementation of the SCG unit. We made a study of the logic designs suggested for the SCG unit of conventional and BEC-based CSLAs of [6] by suitable logic expressions. The main objective of this study is to identify redundant logic operations and data dependence. Accordingly, we remove all redundant logic operations and sequence logic operations based on their data dependence.

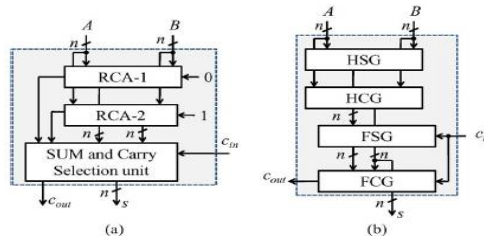


Fig. 3. (a) Conventional CSLA;  $n$  is the input operand bit-width. (b) The logic operations of the RCA is shown in split form, where HSG, HCG, FSG, and FCG represent half-sum generation, half-carry generation, full-sum generation, and full-carry generation, respectively.

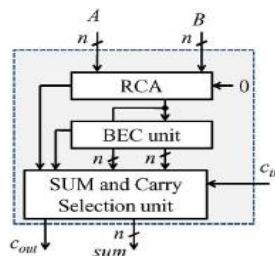


Fig. 4. Structure of the BEC-based CSLA;  $n$  is the input operand bit-width.

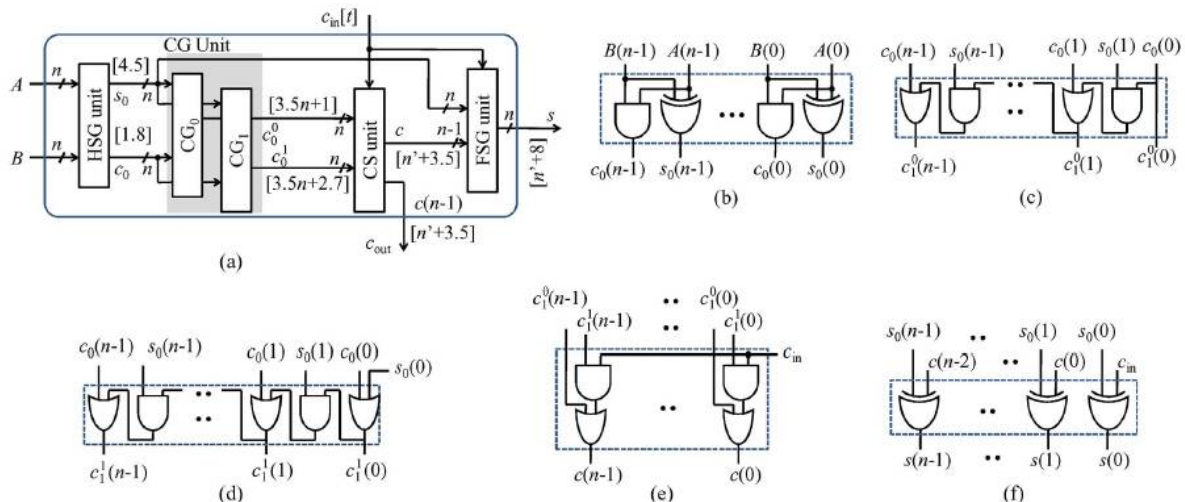


Fig. 5. (a) Proposed CS adder design, where  $n$  is the input operand bit-width, and  $[*]$  represents delay (in the unit of inverter delay),  $n = \max(t, 3.5n + 2.7)$ . (b) Gate-level design of the HSG. (c) Gate-level optimized design of (CG0) for input-carry = 0. (d) Gate-level optimized design of (CG1) for input-carry = 1. (e) Gate-level design of the CS unit. (f) Gate-level design of the final-sum generation (FSG) unit.

The existing CSLA is based on the logic formulation given in (4a)–(4g), and its structure is shown in Fig. 5(a). It consists of one HSG unit, one FSG unit, one CG unit, and one CS unit. The CG unit is composed of two CGs (CG0 and CG1) corresponding to input-carry ‘0’ and ‘1’. The HSG receives two  $n$ -bit operands ( $A$  and  $B$ ) and generate half-sum

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word  $s_0$  and half-carry word  $c_0$  of width  $n$  bits each. Both CG0 and CG1 receive  $s_0$  and  $c_0$  from the HSG unit and generate two  $n$ -bit full-carry words  $c_{01}$  and  $c_{11}$  corresponding to input-carry '0' and '1', respectively. The logic diagram of the HSG unit is shown in Fig. 5(b). The logic circuits of CG0 and CG1 are optimized to take advantage of the fixed input-carry bits. The optimized designs of CG0 and CG1 are shown in Fig. 5(c) and (d), respectively. The CS unit selects one final carry word from the two carry words available at its input line using the control signal  $c_{in}$ . It selects  $c_{01}$  when  $c_{in} = 0$ ; otherwise, it selects  $c_{11}$ . The CS unit can be implemented using an  $n$ -bit 2-to-1 MUX. However, we find from the truth table of the CS unit that carry words  $c_{01}$  and  $c_{11}$  follow a specific bit pattern. If  $c_{01}(i) = '1'$ , then  $c_{11}(i) = 1$ , irrespective of  $s_0(i)$  and  $c_0(i)$ , for  $0 \leq i \leq n - 1$ . This feature is used for logic optimization of the CS unit. The optimized design of the CS unit is shown in Fig. 5(e), which is composed of  $n$  AND-OR gates. The final carry word  $c$  is obtained from the CS unit. The MSB of  $c$  is sent to output as  $c_{out}$ , and  $(n - 1)$  LSBs are XORed with  $(n - 1)$  MSBs of half-sum ( $s$ ) in the FSG [shown in Fig. 3(f)] to obtain  $(n - 1)$  MSBs of final-sum ( $s$ ). The LSB of  $s_0$  is XORed with  $c_{in}$  to obtain the LSB of  $s$ .

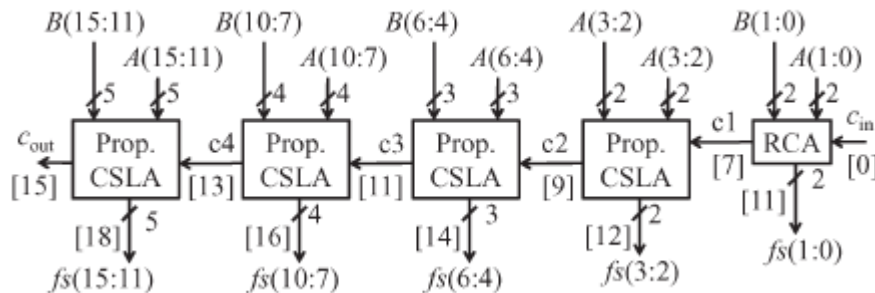


Fig. 6. Proposed Sqrt-CSLA for  $n = 16$ . All intermediate and output signals are labeled with delay

## IV. PROPOSED METHOD

Quantum Dot Cellular Automata (sometimes referred to simply as quantum cellular automata, or QCA) are proposed models of quantum computation, which have been devised in analogy to conventional models of cellular automata introduced by von Neumann. Standard solid state QCA cell design considers the distance between quantum dots to be about 20 nm, and a distance between cells of about 60 nm. Just like any CA, Quantum (-dot) Cellular Automata are based on the simple interaction rules between cells placed on a grid. A QCA cell is constructed from four quantum dots arranged in a square pattern. These quantum dots are sites electrons can occupy by tunneling to them.

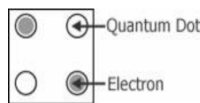


Fig 7: Simplified Diagram of QCA Cell

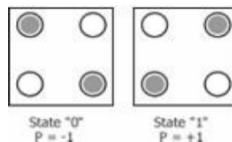


Fig 8: Four Dot Quantum Cell

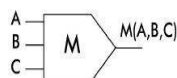


Fig 9: Structure of Majority gate

The QCA majority gate performs a three-input logic function. Assuming the inputs are A, B and C, the logic function of the majority gate is

$$M = AB + BC + CA$$

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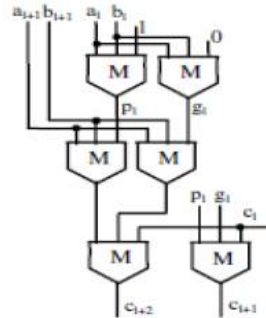


Fig 10: ARCHITECTURE OF BASIC NOVEL 2-BIT ADDER

To introduce the novel architecture proposed for implementing ripple adders in QCA, let consider two  $n$ -bit addends  $A = a_{n-1}, \dots, a_0$  and  $B = b_{n-1}, \dots, b_0$  and suppose that for the  $i$ th bit position (with  $i = n - 1, \dots, 0$ ) the auxiliary propagate and generate signals, namely  $p_i = a_i + b_i$  and  $g_i = a_i \cdot b_i$ , are computed.  $c_i$  being the carry produced at the generic  $(i-1)$ th bit position, the carry signal  $c_{i+2}$ , furnished at the  $(i+1)$ th bit position.

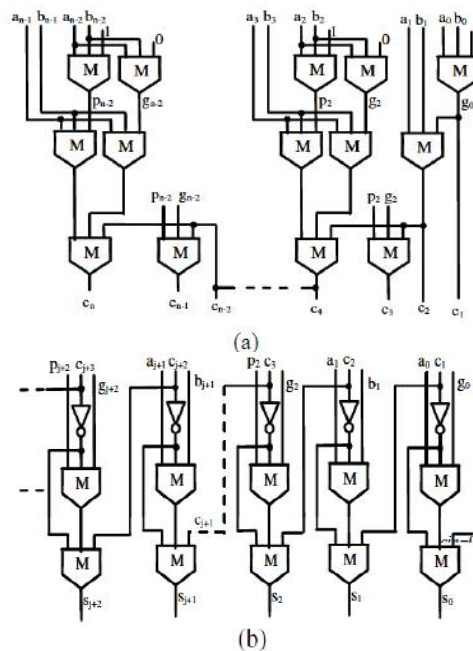


Fig 11: Novel  $n$ -bit adder (a) carry chain and (b) sum block.

And also here we are designed multiplier and accumulator unit by using the existing and proposed CSLA.

## V. SIMULATION RESULTS

The below figures 12,13 shows that output waveforms for SQRT CSLA and the same implementation designed for QCA based adder. According to the synthesis reports in terms of area delay power the proposed QCA adder is more efficient compared to existing conventional based CSLA adders. In extra multiplier synthesis reports are also generated.



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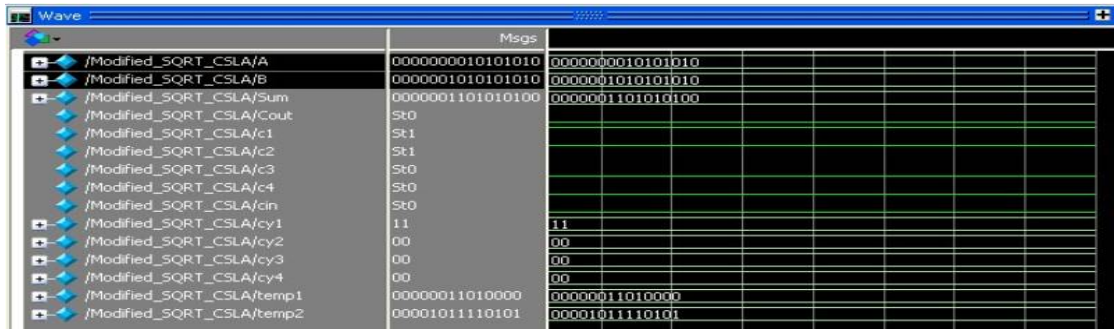


Fig 12: Output waveform for Sqrt CSLA

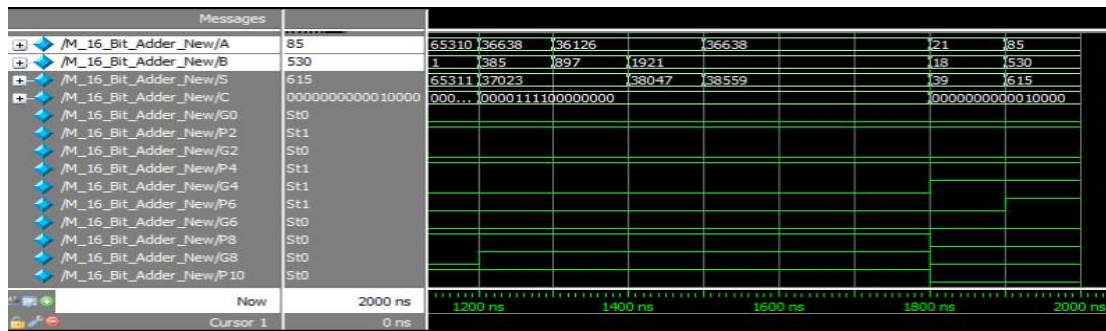


Fig 13: Output waveform for Proposed QCA Adder

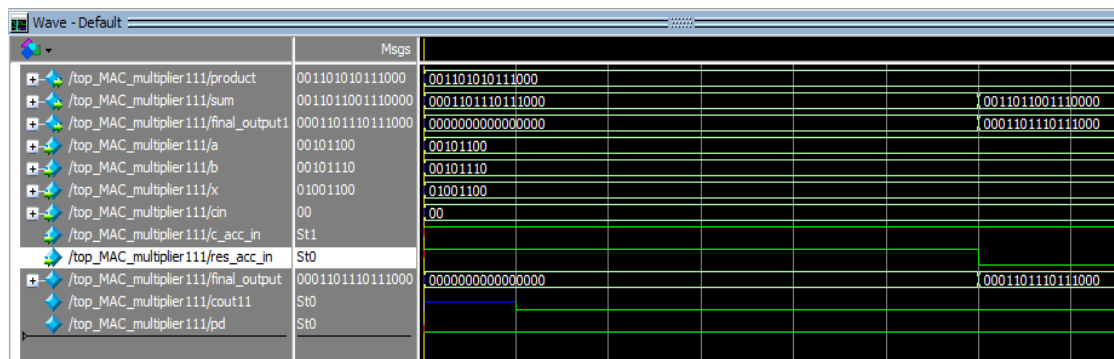


Fig 14: Output waveform for Multiplier and Accumulator

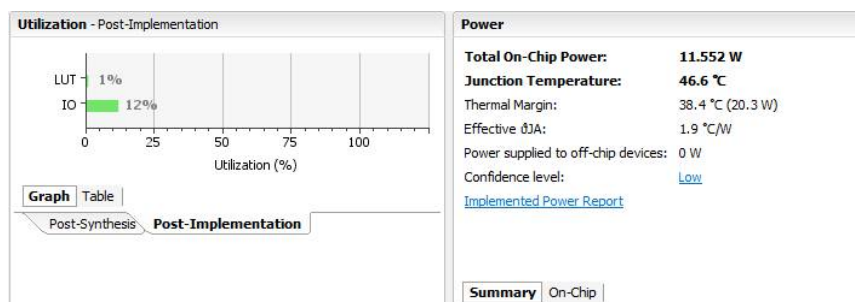


Fig 15: Synthesis report for existing adder

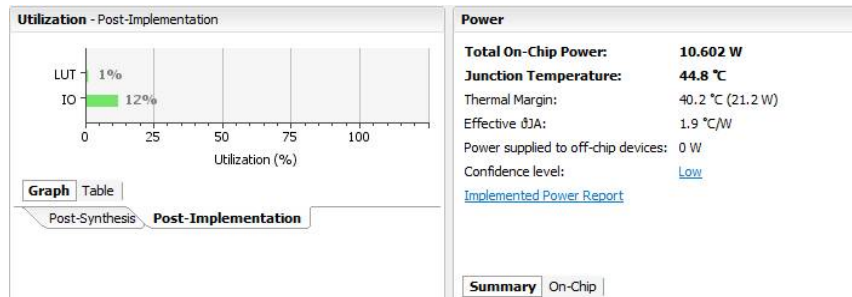


Fig 16: Synthesis report for proposed QCA adder

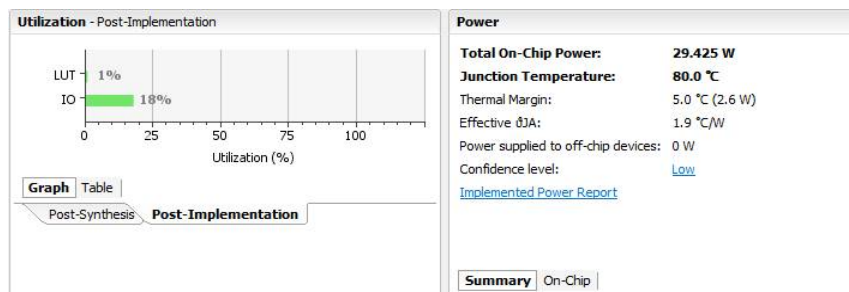


Fig 17: synthesis report for proposed multiplier and accumulator

## VI. CONCLUSION

The reduced number of gates of this work offers the great advantage in the reduction of area and also the total delay. The QCA architecture is therefore, low area, low delay, simple and efficient for VLSI hardware implementation. And we have also analyzed the logic operations involved in the conventional and BEC-based CSLAs to study the data dependence and to identify redundant logic operations. We have eliminated all the redundant logic operations of the conventional CSLA and proposed a new logic formulation for the CSLA. In the proposed scheme, the CS operation is scheduled before the calculation of *final-sum*, which is different from the conventional approach. Carry words corresponding to input-carry '0' and '1' generated by the CSLA based on the proposed scheme follow a specific bit pattern, which is used for logic optimization of the CS unit. Fixed input bits of the CG unit are also used for logic optimization. Based on this, an optimized design for CS and CG units are obtained. Using these optimized logic units, an efficient design is obtained for the existed CSLA. The CSLA design involves significantly less area and delay than the recently proposed BEC-based CSLA. Due to the small carry output delay, the proposed CSLA design is a good candidate for the SQRT adder.

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