

(An ISO 3297: 2007 Certified Organization)

Vol. 5, Issue 1, January 2016

# Sensorless Vector Control of Induction Motor Based On Extended Kalman Filter and Fuzzy Controller

Bineet Kumar Khampariya, Manvendra Singh Kaurav

Research Scholar, Dept. of Electrical Engineering, LNCT, Bhopal, M.P, India Assistant Professor, Dept. of Electrical Engineering, LNCT, Bhopal, M.P, India

ABSTRACT: This paper depicts the vector control of an induction motor by the speed estimation utilizing an extended Kalman filter and fuzzy controller. In this paper, the rotor speed is viewed as a parameter, and the composite state is made out of the first state and the rotor speed. The extended Kalman filter is utilized to distinguish the speed of an induction motor and rotor flux in light of the deliberate amounts, for example, stator currents and DC join voltage. The assessed speed is utilized for vector control and general speed control. The current control is performed at synchronous rotating reference frame, and the assessed speed data is utilized for reference frame transformation of the current controller. PC reproduction of the speed control has been completed to affirm the speed's helpfulness estimation calculation. The error between the genuine speed and the evaluated speed is inside of a couple rpm even at the low and high speeds.

KEYWORDS: Induction motor, Vector Control, Extended Kalman filter, Fuzzy logic controller.

#### I. INTRODUCTION

In advanced control systems for induction motor drives, shaft mounted tachogenerator, resolver, or computerized shaft position encoder are utilized to get speed data. These bring down the system unwavering quality, particularly in mediocre situations. This displays an issue in the systems where motor speed transducers are not generally accessible. This has prompted a speed sensorless vector control. The customary ways to deal with speed sensorless vector control utilize the strategy for flux and slip estimation utilizing stator currents and voltages [1],[2]. The MRAS strategies are likewise used to gauge the speed of an induction motor [3]. As of late, the Kalman filter calculation is utilized for the parameter estimation of an induction motor [4]-[6], or for the speed estimation of a synchronous and an induction motor [7],[8]. In the speed estimation of an induction motor utilizing an extended Kalman filter calculation, a mechanical comparison is utilized as a part of Kalman filter which need the data about idleness of the motor and load, and just the currents are state variables, so the rakish speed of rotor flux is figured outside the extended Kalman filter. This paper shows an option speed sensorless vector control which utilizes an extended Kalman filter calculation to Appraise the motor speed and rotor flux, and along these lines builds up the vector control and additionally the general speed control. What's more, in this system just the stator currents and DC join voltage is the deliberate amounts. In any case, it is difficult to add to a precise system scientific model because of obscure burden varieties and system disturbances [2]. Accordingly the Fuzzy Logic Control hypothesis (FLC) is generally utilized for the motor control purpose [5]. FLC is taking into account fuzzy set hypothesis, presented by Zadeh.[4].FLC does not require any accurate system numerical model and it can deal with nonlinearity of discretionary multifaceted nature and it is in view of the semantic guidelines. In this paper the Induction's speed motor which is running in Simulink/Matlab environment is assessed just by measuring the three phase stator data currents. What's more, with this assessed speed data, a fuzzy logic control system is created so that the motor's speed can be controlled accurately.



ISSN (Print) : 2320 – 3765 ISSN (Online) : 2278 – 8875

# International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

#### Vol. 5, Issue 1, January 2016

#### II. MATHEMATICAL MODEL OF INDUCTION MOTOR

As generally iron losses, saturation of the electromagnetic circuit are ignored when adding to the scientific model of the induction motor. A dynamical model of induction motor in a stationary reference frame, by picking the stator currents  $i_{\alpha}$ ,  $i_{\beta}$  and the rotor flux $\psi_{r\alpha}$ ,  $\psi_{r\beta}$  and the motor precise speed  $\omega$  r as state variables is

Where *x* is the state vector.

Where

$$R_s, R_r$$
: Stator and Rotor resistances.

 $L_s, L_r$ : Stator and Rotor self inductances.

 $L_m$ : Mutual inductance. The two axis stator voltages and currents in synchronously rotating frame are related to the three phase representations by the following equation:



(An ISO 3297: 2007 Certified Organization)

#### Vol. 5, Issue 1, January 2016

$$\begin{bmatrix} f_{qs}^e \\ f_{ds}^e \end{bmatrix} = \begin{bmatrix} -\sin(\omega_e t) & \cos(\omega_e t) \\ \cos(\omega_e t) & \sin(\omega_e t) \end{bmatrix} \begin{bmatrix} \frac{2}{3} & -\frac{1}{3} & -\frac{1}{3} \\ 0 & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{3}} \end{bmatrix} \begin{bmatrix} f_{as} \\ f_{bs} \\ f_{cs} \end{bmatrix}$$

where f may represent either the voltage or current.  $\omega_e$  is the synchronous speed.

where  $\omega_{sl}$  is the slip speed and  $\omega_r$  is the rotor speed. Thefield oriented control requires to keep the magnetizing current at a constant rated value by setting  $i_{dr}^e = 0$  Hence theorem producing current component can be adjusted inaccordance with the torque demand. The electromagnetic torque,

where  $\lambda_{dr}$  is the *d* axis rotor flux linkage.

#### III. EXTENDED KALMAN FILTER (EKF) ALGORITHM

In the dynamic model of induction motor, if the dimension of state vector is increased by adding an angular speed of rotor, then thestate model between nonlinear. So the extended Kalmanfilter has tobeused to estimate the parameter. In this case, the angular speedof the rotor is considered as a stateand a parameter. For the applicability of extended Kalman filter the system should be expressed in discrete state. The discrete state model and the output model are given by:

$$X(k + 1) = f[X(k), k] + G(k)w(k), \dots \dots \dots \dots \dots (8)$$
  

$$Y(k) = H(k)X(k) + v(k), \dots \dots \dots \dots (9)$$

Where

G(k) =Weighting matrix.

w(t) =Noise matrix of state model.

v(t) =Nose matrix of output model.

In this model f[X(k), k] is the nonlinearpart of state model. The extended Kalman filter re-linearize the nonlinear state model about each new estimate as it becomes available, and the new discrete state model and output model is described by Eq. (10),(11).

Where

$$F(k) = \frac{\delta f[x(k), k]}{\delta k} \bigg|_{x=x(k+1|k)}$$
$$s(k) = f[x(k+1|k)] - F(k)x(k+1|k)$$

From the above dynamic model therotor speed can be estimated by the following extended Kalman filter algorithm. Estimation of error covariance matrix:

$$(k+1|k) = \Phi(k+1,k)P(k|k)\Phi^{T}(k+1,k) + Q_{d}(k)$$

Computation of Kalman filter gain:

$$K(k+1) = \frac{P(k+1|k)H^{T}(k+1)}{[H(k+1)P(k+1)H^{T}(k+1) + R(k+1)]}$$

Update for error covariance matrix:

$$P(k+1|k+1) = [I - K(k+1)H(k+1)]P(k+1|k)$$

State estimation:

$$x(k+1|k+1) = x(k+1|k) + K(k+1)(z(k+1) - h[x(k+1|k,k+1])$$



(An ISO 3297: 2007 Certified Organization)

#### Vol. 5, Issue 1, January 2016

#### IV. ESTIMATION OF ROTOR SPEED BY EXTENDED KALMAN FILTER ALGORITHM

Let the state variablesbe defined as followings.

$$\begin{bmatrix} x_1(t) \\ x_2(t) \\ x_3(t) \\ x_4(t) \\ x_5(t) \end{bmatrix} = \begin{bmatrix} i_{ds}(t) \\ i_{qs}(t) \\ \phi_{dr}(t) \\ \phi_{dq}(t) \\ \omega_r(t) \end{bmatrix}$$

Then the state model of the induction motor can be given as

$$x(t) = f[x(t), u(t), t] + Q(t)w(t)$$

Where

$$f[x(t), u(t), t] = [f_{1}(t), f_{2}(t), f_{3}(t), f_{4}(t), f_{5}(t)]^{T}$$

$$= \begin{bmatrix} -\left(\frac{R_{s}}{\sigma L_{s}} + \frac{1 - \sigma}{\sigma \tau_{r}}\right)x_{1} + \frac{L_{m}}{\sigma L_{r}L_{s}\tau_{r}}x_{3} + \frac{L_{m}}{\sigma L_{s}L_{r}}x_{4}x_{5} + \frac{1}{\sigma L_{s}}V_{ds}f \\ -\left(\frac{R_{s}}{\sigma L_{s}} + \frac{1 - \sigma}{\sigma \tau_{r}}\right)x_{2} + \frac{L_{m}}{\sigma L_{r}L_{s}}x_{2}x_{5} + \frac{L_{m}}{\sigma L_{s}L_{r}}\tau_{r}}x_{4}x_{5} + \frac{1}{\sigma L_{s}}V_{ds}f \\ \frac{L_{m}}{\tau_{r}}x_{1} - \frac{1}{\tau_{r}}x_{3} - x_{4}x_{5} \\ \frac{L_{m}}{\tau_{r}}x_{2} + x_{3}x_{5} - \frac{1}{\tau_{r}}x_{4} \\ \sigma = 1 - \frac{L_{m}}{L_{s}L_{r}} \\ G(t) = \begin{bmatrix} \frac{1}{\sigma L_{s}} & 0 & 0 \\ 0 & \frac{1}{\sigma L_{s}} & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \frac{1}{\sigma} \end{bmatrix} \\ w(t) = \begin{bmatrix} w_{1}(t) \\ w_{2}(t) \\ n(t) \end{bmatrix}$$

And the output matrix is given as follows

 $z(t_1) = h[x(t_i), t_i] + v(t_i)$ 

Where

$$z(t_i) = \begin{bmatrix} i_{ds}(t) \\ i_{qs}(t) \end{bmatrix}$$
$$h[x(t_i), t_i] = \begin{bmatrix} i_{ds}(t_i) \\ i_{qs}(t_i) \end{bmatrix}$$

 $x(t_0)$  is the initial condition with mean  $x_0$  and covariance  $P_0$ , and u(t) is deterministic input, w(t) is a zero mean white Gaussian noise that is independent of  $x(t_0)$  with covariance Q(t). v(t) is zero mean white Gaussian noise that is independent of  $x(t_0)$  and w(t) with covariance  $R(t_i)$ . The extended Kalman filter prediction equation is given by



(An ISO 3297: 2007 Certified Organization)

#### Vol. 5, Issue 1, January 2016

 $\hat{x}(k+1|k) = \hat{x}(k|k) + \int_{t_k}^{t_{k+1}} f[x(t|t_k), u(t), t] dt$ In this case u(t) is assumed to be constant between  $t_k$  and  $t_{k+1}$ . The updated covariance is given by:  $P(k+1|k)P(k|k)\Phi^{T}(k+1|k) + Q_d(k)$ 

Where

$$\begin{split} \Phi(k+1|k) &= e^{F(k)T_s}, T_s = sampling \ time\\ Q_d &= \int \Phi(t_{k+1}, \tau) G(\tau) Q(\tau) G^T(\tau) \Phi^T(t_{k+1}, \tau) d\tau\\ F[k+1] &= \frac{\delta f[x(t), u(t), t]}{\delta x} \bigg|_{x=x(k+1|k)}\\ &= \begin{bmatrix} -\left(\frac{R_s}{\sigma L_s} + \frac{1-\sigma}{\sigma \tau_r}\right) \ 0 \ \frac{L_m}{\sigma L_r L_s \tau_r} \frac{L_m}{\sigma L_s L_r} x_5 \frac{1}{\sigma L_s L_r} x_4\\ 0 \ -\left(\frac{R_s}{\sigma L_s} + \frac{1-\sigma}{\sigma \tau_r}\right) x_2 \frac{-L_m}{\sigma L_r L_s} x_5 \frac{L_m}{\sigma L_s L_r \tau_r} \frac{1}{\sigma L_s L_r} x_2\\ \frac{L_m}{\tau_r} \ 0 \ \frac{-1}{\tau_r} \ -x_5 \ -x_4\\ 0 \ \frac{L_m}{\tau_r} x_5 \frac{-1}{\tau_r} x_4 \ -x_3\\ 0 \ 0000 \end{bmatrix} \end{split}$$

The Kalman gain is given by

$$K(k+1) = \frac{P(k+1|k)H^{T}(k+1)}{[H(k+1)P(k+1)H^{T}(k+1) + R(k+1)]}$$

Where

$$H[k+1] = \frac{\delta f[x(t), t]}{\delta x} \bigg|_{x=x(k+1|k)}$$
$$= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \end{bmatrix}$$

#### V. FUZZY LOGIC CONTROLLER

Fuzzy logic is an approach to computer science that mimics the way a humanbrain thinks and solves problems [11]. The idea of fuzzy logic is to approximate decision making using natural language terms instead of quantitative terms. It is generally considered as modeling of information where it cannot be defined precisely, but some broad definitions can be formed. Because of its simplicity and effectiveness, Fuzzy-logic technology has gained many applications in scientific and industrial applications.

A typical architecture of FLC is shown below, which comprises of four principal comprises: a fuzzifier, a fuzzy rule base, inference engine, and a defuzzifier.

*Fuzzifier:* Used to transform crisp measured data (e.g. speed is 10 mph) into suitable linguistic values (i.e. fuzzy sets, for example, speed is too slow).

Fuzzy Rule Base: stores the empirical knowledge of the operation of the process of the domain experts.

*Inference Engine:* is the kernel of a FLC, and it has the capability of simulating human decision making by performing approximate reasoning to achieve a desired control strategy.

*Defuzzifier:* is utilized to yield a non fuzzy decision or control action from an inferred fuzzy control action by the inference engine.



(An ISO 3297: 2007 Certified Organization)

#### Vol. 5, Issue 1, January 2016

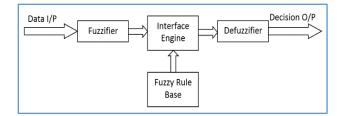


Figure 1: Block Diagram of Fuzzy Controller

#### VI. THE MODEL EXPLOITATION

The block diagram of the model is presented in figure 2. The EKF estimates the rotor speed  $\omega_r$  using the three phase statorcurrents. The rotor speed is compared with the set speed toproduce the error in the speed. For the proposed FLC thespeed error and the rate of change of the speed error areconsidered as the input linguistic variables and the torqueproducing current component  $i_{as}^{e}$  is considered as the output linguistic variable. The change of speed error

And the speed error

$$\Delta e(n) = \Delta \omega_{\rm r}(n) - \Delta \omega_{\rm r}(n-1)$$

 $\Delta \omega_{\rm r}(n) = \Delta \omega_{\rm r}^*(n) - \Delta \omega_{\rm r}(n)$ 

Using these equations, the synchronous speed  $\omega_e$  is calculated assuming a value for slip. The rotor position  $\theta_e$  is determined by integrating the synchronous speed. With theinformation of the rotor position the three phase statorcurrents are converted into synchronously rotating frame  $\hat{t}_{qs}^e$  and  $\hat{t}_{ds}^e$ . The quadrature axis current,  $\hat{t}_{qs}^e$  generated by FLC is compared with the estimated q axis current and

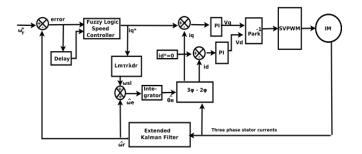


Figure 2: The block diagram representation of the proposed controller.

the error in q axis current is passed through a PI controller to get q axis voltage  $v_{qs}^e$ . The d axis current is set to zero which then compares with the estimated d axis current and passed through a PI controller to produce d axisvoltage. Then they undergo an inverse PARK transformation. A space vector PWM inverter is used to drive the Induction motor.

#### VII. SIMULATION AND RESULTS ANALYSIS

In the proposed vector control system, the voltage control is performed at synchronously rotating reference frame. The motor speed  $\omega_r$  is estimated using the EKF algorithm. The model is developed and simulated in Matlab/Simulink environment.



(An ISO 3297: 2007 Certified Organization)

#### Vol. 5, Issue 1, January 2016

Table 1: The specifications of the Inductionmotor used is:

Parameter	Value
Voltage	460V
Frequency	50Hz
Power	50HP
$R_s$	0.087Ω
$R_r$	0.228Ω
L <sub>s</sub>	0.0008H
L <sub>r</sub>	0.0008H
L <sub>m</sub>	0.034H
J	1.662
$B_m$	0.1

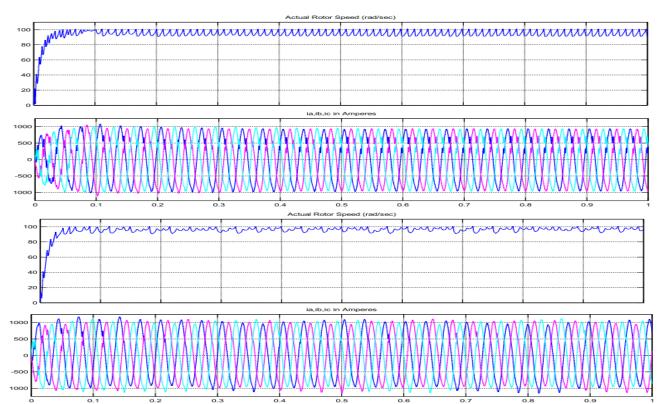


Figure 3: actual motor speed and phase currents in previous (top two graphs) and proposed technique (bottom two graphs). Comparison between the previous method and the proposed method on the basis of figure 3. Reveals that the speed fluctuations and the current ripple in proposed method are much less, compared to the previous scheme.



(An ISO 3297: 2007 Certified Organization)

#### Vol. 5, Issue 1, January 2016

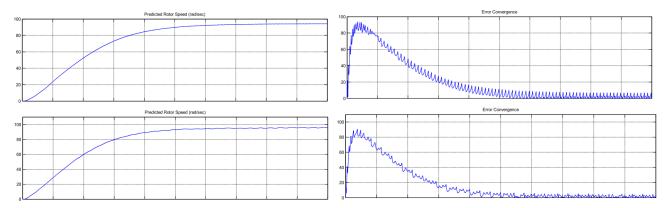


Figure 4: Motor speed estimation and estimation error convergence in previous (top graph) and proposed (bottom graph) technique.

The figure 4 graphs shows that the speed estimation in proposed technique is much better and quick responding. While the error converges much smoothly and quickly in the proposed technique.

#### VIII. CONCLUSION

An EKF estimator alongside FLC sensorless speed controller of an induction motor has been effectively simulated in Matlab/Simulink environment. The execution truly demonstrates that the controller can be utilized as a part of precise speed controller. The outcomes shows the efficacy of the Extended Kalman filter calculation for estimation purposes. The estimator is steady and fast for every single set speed. The FLC could follow and achieve all the set speeds rapidly. FLC has demonstrated its incredibleness in taking care of indeterminate parameters and unsettling influences. The controller execution has been tried for different step changes in speed in Simulink environment and discovered the same accuracy level in tracking them.

#### REFERENCES

[1] Bindu V, Unnikrishnan A and Gopika kumari R. "Fuzzy logic based sensorless vector control of Induction motor", India Conference (INDICON), 2012 Annual IEEE7-9 Dec. 2012.

[2] Young-Real Kim, Seung-Ki Sul, Min-Ho Park "peed Sensorless Vector Control of an Induction Motor Using an Extended Kalman Filter" Industry Applications, IEEE Transactions on (Volume:30, Issue: 5), Sep/Oct 1994.

[3] J. W. Finch and D. Giaouris, "Controlled ac electrical drives," IEEE Trans.Ind. Electron., vol. 55, no. 2, pp. 481–491, Feb. 2008.

[4] C. Patel, R. Ramchand, K. Sivakumar, A. Das, and K. Gopakumar, "Arotor flux estimation during zero and active vector periods using currenterror space vector from a hysteresis controller for a sensorless vectorcontrol of IM drive," IEEE Trans. Ind. Electron., vol. 58, no. 6, pp. 2334–2344, Jun. 2011.

[5] T. Orlowska-Kowalska and M. Dybkowski, "Stator-current-based MRASestimator for a wide range speed-sensorless induction-motor drive," IEEETrans. Ind. Electron., vol. 57, no. 4, pp. 1296–1308, Apr. 2010.

[6] Y. M. Choi and D. G. Gweon, "A high-precision dual-servo stage usingHalbach linear active magnetic bearings," IEEE/ASME Trans. Mechatronics., vol. 16, no. 5, pp. 925–931, Oct. 2011.

[7] T. Schuhmann, W. Hofmann, and R. Werner, "Improving operational performance of active magnetic bearings using Kalman filter and state feedback control," IEEE Trans. Ind. Electron., vol. 59, no. 2, pp. 821–829, Feb. 2012.

[8] I. U. R. Usman, M. Paone, K. Smeds, and X. D. Lu, "Radially biased axial magnetic bearings/motors for precision rotary-axial spindles," IEEE/ASME Trans. Mechatronics, vol. 16, no. 3, pp. 411–420, Jun. 2011.