

# Mathematical Modeling of Grid Connected PV System Using S-Transforms

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**ABSTRACT:** This paper presents the mathematical modeling of PV system connected to grid with S-transforms. Mathematical modeling of power electronic converters is an issue for power engineers from long time. Conventional modeling goes away from using transfer functions due to the involvement of high degree non-linearity in power converters. In this paper, mathematical modeling of grid connected PV system was developed using S-transforms. Three phase outputs were shown for grid connected PV system.

**KEYWORDS:** PV, Modeling, Power Converter, Grid.

## I. INTRODUCTION

Reducing global warming, improved public health and environment quality, vast and inexhaustible energy supply, economic supply and stable energy supply makes renewable energy a prospect for electrical energy generation. Renewable energy is classified as energy that comes from resources like sun light (known as solar), wind, geo-thermal heat and rain that are constantly replenished. Renewable energy can serve as a replacement to electricity, motor fuels, rural energy and heating. Solar and wind are mostly used and solar is the dominant renewable energy source being used. Since the evolution of power electronic converters, engineers have tried to develop different mathematical models and analysis techniques with their respective control circuits for different power converters. Modelling based on small signal analysis was used most. This methodology uses power converter circuits for development of mathematical models. This method fails to predict the fast dynamics of the converters whereas they are very good in sensing slow dynamics.

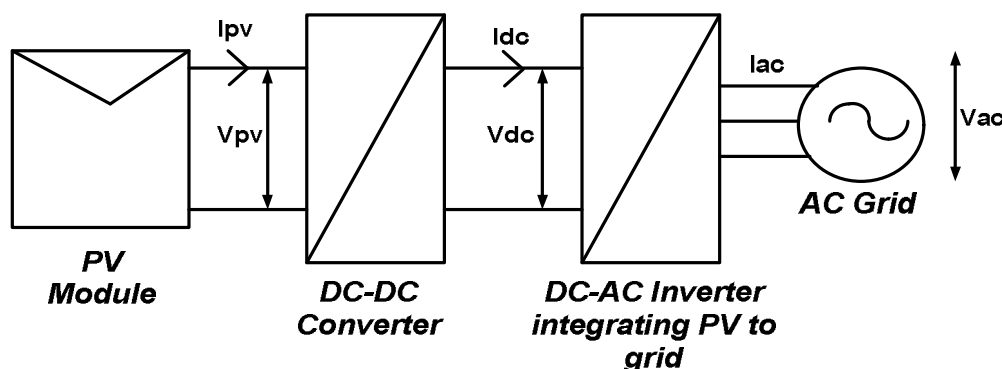


Fig.1: System with PV integration to utility Grid

In transfer function model, an initial assumption is made in parameter identification. But the transfer function derivation of power converters in S-domain using Laplace transforms is limited by non-linear characteristics of converters. Non-linearity is introduced due to the switches in the power converters. In this paper a simple transfer function was developed along with the transfer functions of DC-DC converter and inverter transfer function. Combining all the three transfer functions of PV, DC-DC and inverter the overall transfer function can be obtained for the system PV integrated to grid.

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## II. GRID CONNECTED PV SYSTEM

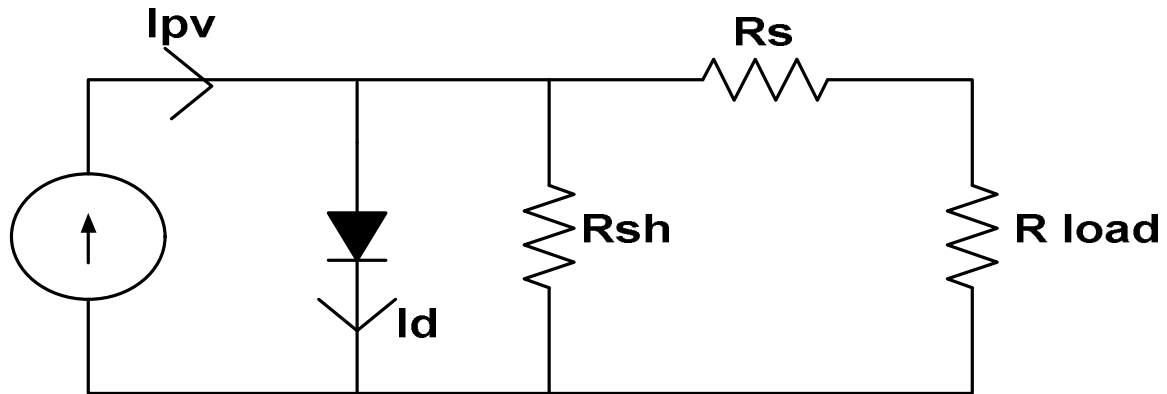


Fig.2: PV string equivalent circuit

Grid connected PV equivalent was shown in figure 2 and consists of current source, anti-parallel diode, shunt resistance due to leakage current and series resistance. Current through diode is  $I_d$  and current from PV is  $I_{pv}$ . PV array is formed by connecting all the PV strings in series. Each PV string looks like in figure 2. The current from PV cell is given by

$$I_{pv} = I_0 \left[ \exp \left( \frac{q(V - IR_s)}{kT} \right) - 1 \right] \quad (1)$$

where  $k$  is Boltzmann constant,  $T$  is the temperature,  $R_s$  is the equivalent series resistance of the array,  $R_{sh}$  is the shunt resistance of the PV array due to leakage current,  $I_0$  is the reverse saturation current of PV cell.

Generally the output of PV cell is connected to a DC-DC converter. The output of PV system will be a low-voltage output and this low-voltage output needs to be increased to a desired value. The DC-DC converter performs this task of step-up low voltage to required desired voltage.

## III. TRANSFER FUNCTION DERIVATION

(a) The transfer function of the PV array current to the instantaneous power is given by

$$\frac{p(s)}{I_{pv}(s)} = \frac{p(s)}{i_{ac}(s)} \frac{i_{ac}(s)}{I_{pv}(s)} = \frac{p(s)}{i_{ac}(s)} \frac{i_{ac}(s) I_{dc}(s)}{I_{dc}(s) I_{pv}(s)} \quad (2)$$

$$= \frac{2S^2}{M_1 M_2 (S^2 + 4\omega^2)} \frac{V_m (S^2 + \omega^2) S^2 + \omega^2}{S^2 (S^2 + 4\omega^2)} \quad (3)$$

The transfer function from the solar panel's input current to the output of the averaging module,  $P$  can be written as shown in eqn. (4)

$$\frac{p}{I_{pv}} = \frac{S^2}{(S^2 + \omega^2)} \frac{V(S^2 + \omega^2)(S^2 + 2\omega^2)}{KS^2(S^2 + 4\omega^2)} \frac{(1 - e^{-sT_s})}{sT_s} \quad (4)$$

Simplified transfer function for PV cell can be written as

$$\frac{I_{pv}}{\text{solar irradiation}} = k \quad (5)$$

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(b) Transfer function of a boost converter:

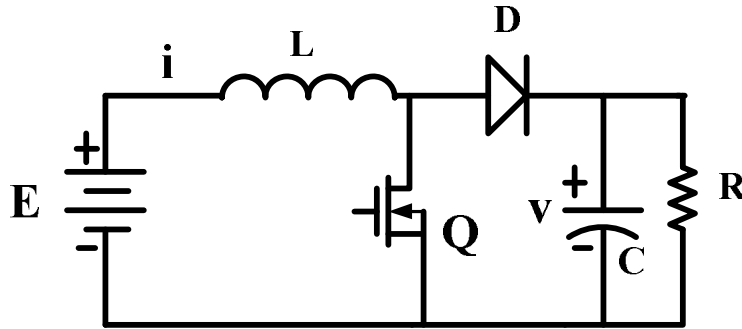


Fig.3: Boost converter

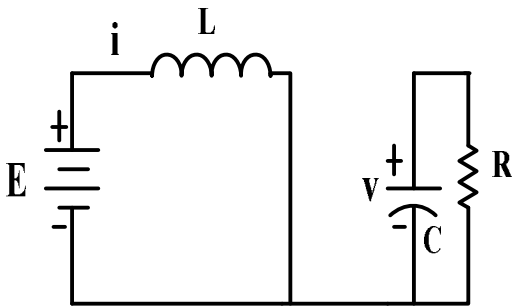


Fig.4: Boost converter when switch is closed

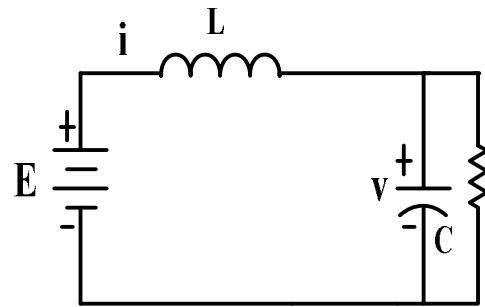


Fig.5: Boost converter when switch is open

When the switch position function is set to  $u = 1$ , we obtain, using Kirchoff's voltage and Kirchoff's current laws, the dynamics described by the following set of equations,

$$L \frac{di}{dt} = E \tag{6}$$

$$C \frac{dv}{dt} = -\frac{v}{R} \tag{7}$$

When the switch position function is set to  $u = 0$ , we obtain the dynamics described by the equations,

$$L \frac{di}{dt} = -V + E \tag{8}$$

$$C \frac{dv}{dt} = i - \frac{v}{R} \tag{9}$$

The Boost converter dynamics is then described by the following *bilinear* 1 type of system:

$$L \frac{di}{dt} = -(1 - u)V + E \tag{10}$$

$$C \frac{dv}{dt} = (1 - u)i - \frac{v}{R} \tag{11}$$

However, transfer function of a boost converter in real time implementation can be written more precisely as shown in the below equation [4]-[6]

$$G'_1(s) = \frac{H_1}{1 + s\frac{L}{R} + s^2LC} = \frac{\frac{H_1}{LC}}{s^2 + \frac{s}{RC} + \frac{1}{LC}} \tag{12}$$

Here,  $R$  is the output resistance seen by the dc-dc converter and can be written as shown in eqn.(13)

$$R = \frac{V_2^2}{P} = \frac{P}{I_2^2} \tag{13}$$

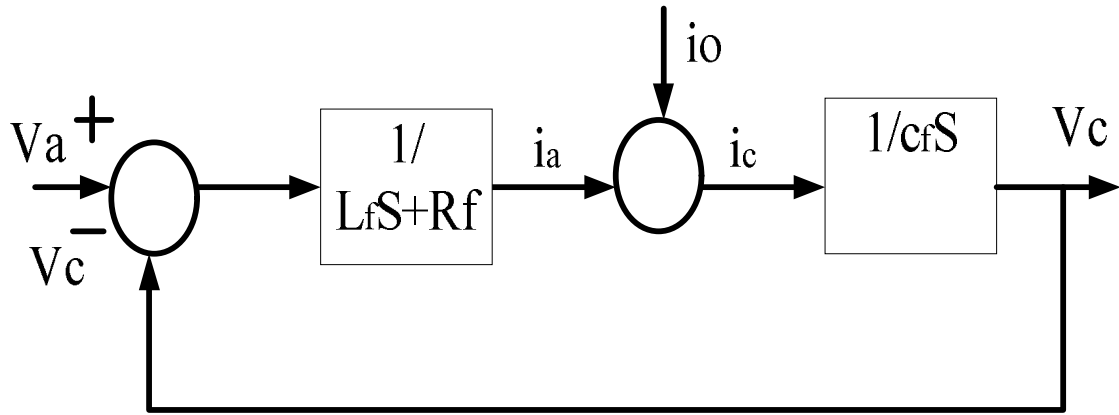


Fig.6: Block diagram of single phase inverter

(C) Figure 6 shows the system block diagram of the single phase inverter the input and output transfer function of inverter is:

$$V_C(S) = \frac{1}{L_f C_f S^2 + j R_f C_f} V_A(s) - \frac{L_f S + R_f}{L_f C_f S^2 + j R_f C_f + 1} I_o(S) \quad (14)$$

The frequency transfer function can be expressed as

$$V_C(j\omega) = \frac{1}{1 - L_f C_f \omega^2 + j R_f C_f \omega} v(j\omega) - \frac{j L_f \omega + R_f}{1 - L_f C_f \omega^2 + j R_f C_f \omega} I_o(j\omega) \quad (15)$$

To determine the transfer function:

$$V_a(S) - s L_f I_a(S) - R_f I_a(S) - V_c(S) = 0 \quad (16)$$

$$V_a(S) - V_c(S) = I_a(S)(s L_f + R_f) \quad (17)$$

$$\frac{V_a(S)}{V_c(S)} = 1 + \frac{I_a(S)(s L_f + R_f)}{V_c(S)} \quad (18)$$

$$\frac{V_a(S)}{V_c(S)} = 1 + \frac{I_a(S)(s L_f + R_f) s C_f}{I_c(S)} \quad (19)$$

$$\frac{V_a(S)}{V_c(S)} = \frac{s^2 L_f C_f + s L_f + R_f C_f s Z_L + R_f + Z_L}{Z_L} \quad (20)$$

$$\frac{V_c(S)}{V_a(S)} = \frac{Z_L}{s^2 L_f C_f + s L_f + R_f C_f s Z_L + R_f + Z_L} \quad (21)$$

The overall transfer function of the system consisting of PV system, boost converter and the inverter can be obtained by combining all the three individual transfer functions of PV system, boost converter and inverter as

$$\frac{P}{V_a(s)} = \frac{S^2}{(S^2 + \omega^2)} \frac{V(S^2 + \omega^2)(S^2 + 2\omega^2)}{K S^2 (S^2 + 4\omega^2)} \frac{(1 - e^{-s T_s})}{s T_s} * \frac{H_1}{1 + S \frac{L}{R} + s^2 LC} = \frac{\frac{H_1}{LC}}{S^2 + \frac{S}{RC} + \frac{1}{LC}} * \frac{Z_L}{s^2 L_f C_f + s L_f + R_f C_f s Z_L + R_f + Z_L} \quad (22)$$

## IV.MATLAB/SIMULINK MODEL AND RESULTS

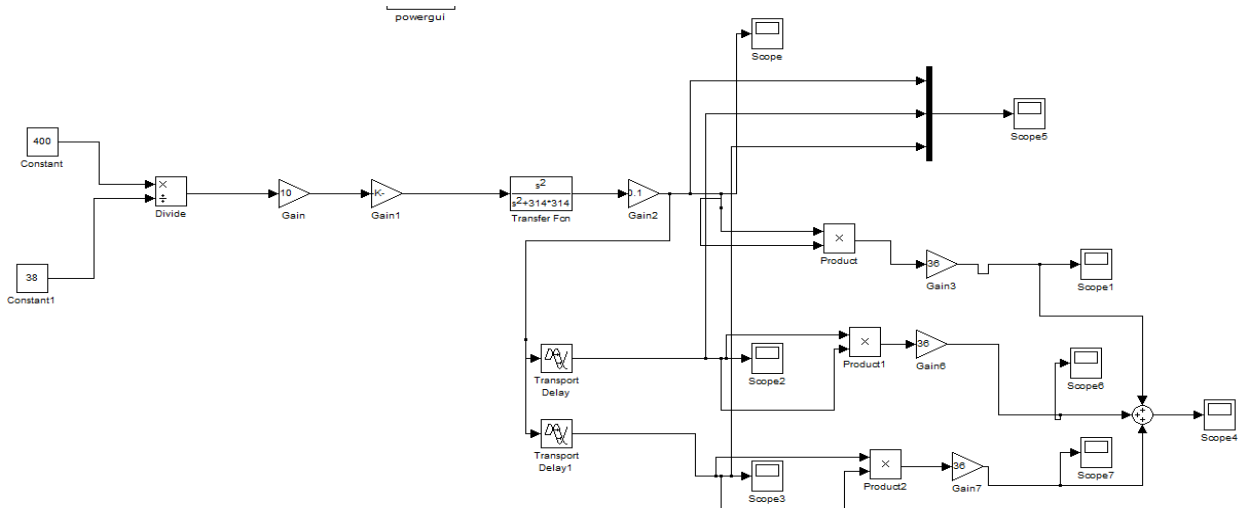


Fig.7: Matlab model of overall system with PV system, Boost converter and inverter for grid connection

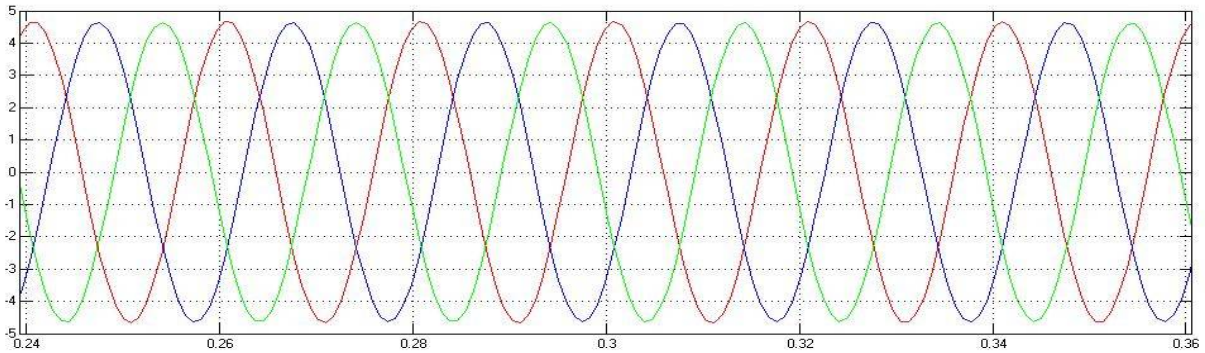


Fig.8: current waveform of the system

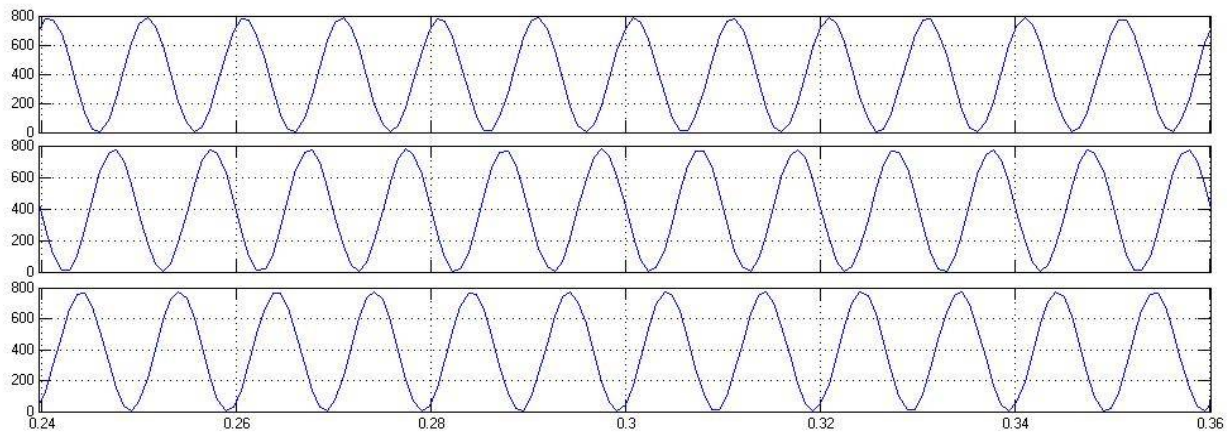


Fig.9: Power waveform of the individual three phases of the system

Figure 7 shows the matlab model of grid connected PV system via boost converter and inverter. Figure 8 shows the current waveform of the system and the power waveforms were shown in figure 9.



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## V.CONCLUSION

This paper presents the mathematical modeling of PV system connected to grid with s-transforms. For a long time, mathematical modeling of power electronic converters is an issue for power engineers. Conventional modeling goes away from using transfer functions due to the involvement of high degree non-linearity in power converters. This paper presents mathematical modeling of grid connected pv system developed using s-transforms. Complete modeling of PV system, boost converter and inverter were shown. The output currents and power of the grid were also shown which were obtained using mathematical modeling.

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