On The Determination of a Low Cost K-Connected Network

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ABSTRACT: The goal of the topological design of a computer network is to achieve a specified performance at a minimal cost. Unfortunately, the problem is completely intractable. A reasonable approach is to generate a potential network topology. One heuristic for generating a potential network topology is due to Steiglitz, Weiner and Kleitman and is called the link deficit algorithm. This paper presents a modified version of the above heuristic which results in a lower cost starting network. In addition, a novel and simple algorithm has been presented for designing a 3-connected starting network when the number of nodes in the network exceeds four.


1. INTRODUCTION

The terms 'K-connected network’, ‘starting network’, ‘link deficit algorithm’, ‘topological design’, ‘minimal spanning tree’ have the usual meanings [1,2,3].

The goal of the topological design of a computer communication network is to achieve a specified performance at a minimal cost. Unfortunately, the problem can be solved only by using exponential algorithms and as such the problem is completely intractable [2]. The fastest available super computers cannot optimize a 25 node network, let alone a 100 node network. Thus, a reasonable approach is to generate a potential network topology (called a starting network) and see if it satisfies connectivity and delay constraints. If not, the starting network is subjected to small modification (called perturbation) to yield a slightly different network, which is now checked to see if it is better. If a better network is found, it is used as the base for more perturbations. If the network resulting from perturbation is not better, the original network is perturbed in some other way. This process is repeated till the computer budget is used up [4, 5].

One of the many heuristics for generating a starting network is the link deficit algorithm [6]. We now present a modified version of the link deficit algorithm which results in a lower cost starting network.

II. MODIFIED LINK DEFICIT ALGORITHM

The geographical positions of the nodes of a network are given. A cost matrix gives The cost of establishing a link between any node i to any node j (i is not equal to j). The minimal spanning tree is determined using Kruskal’s algorithm or Prim’s algorithm [2]. Now the link deficit algorithm is applied to obtain the starting network. We illustrate this novel algorithm by working out an illustrative example [1].
III. ILLUSTRATIVE EXAMPLE

The geographical positions of five nodes labeled 1 through 5 are shown in fig 1.

![Fig 1](image)

The cost of establishing a link between any nodes i to any node j is given by the following cost matrix $C$

\[
C = \begin{pmatrix}
1 & 2 & 3 & 4 & 5 \\
1 & -2 & 2 & 1 & 8 \\
2 & 2 & -4 & 10 & 5 \\
3 & 2 & 4 & -4 & 6 \\
4 & 1 & 10 & 4 & -2 \\
5 & 8 & 5 & 6 & 2
\end{pmatrix}
\]

The minimal spanning tree can be determined as usual [2, 4] and is shown in fig 2. Let us suppose that we want to set up a 3-connected network. In fig 2, the deficits of the nodes 1 through 5 are 0, 2, 2, 1 and 2 respectively. Application of the link deficit algorithm to what is shown in fig 2 results in the starting network shown in fig 3.

![Fig 2](image)

This modified link deficit algorithm can be used to set up any k-connected network wherein K is greater than 1 [3]. We now present a simple algorithm. Wherein the minimal spanning tree algorithm is applied twice [5].
IV. ALGORITHM FOR A 3-CONNECTED NETWORK

Given the geographical positions of the nodes of a network and a cost matrix giving the cost of establishing a link between any node i and any node j, we proceed as follows. The minimal spanning tree $T_1$ is determined. The costs of the link presented in $T_1$ are made infinite in the cost matrix and the minimal spanning tree $T_2$ is again determined [6,7]. A low cost 3-connected starting network results when the edges of $T_1$ and $T_2$ are superimposed. We now illustrate this novel approach by working out the previous example.

V. ILLUSTRATIVE EXAMPLE

The geographical positions of the nodes of a network are shown in fig 1. The cost matrix is given by equation 1. The minimal spanning tree is determined as usual and is shown in fig 2. In the cost matrix given in equation 1, the costs of the edges present in fig 1 are made infinite and the modified cost matrix $C'$ is shown below [8-10].

\[
C' = \begin{bmatrix}
1 & 2 & 3 & 4 & 5 \\
2 & \infty & \infty & \infty & 8 \\
3 & \infty & 4 & 10 & 5 \\
4 & \infty & 10 & 4 & \infty \\
5 & 8 & 5 & 6 & \infty \\
\end{bmatrix}
\]

(2)

For the cost matrix $C'$ given in equation 2, we find the minimal spanning tree as shown in fig 4 [11, 12]. When the edges shown in fig 2 and fig 4 are superimposed, we get a low cost 3 connected starting network as shown in fig 5.
VI. CONCLUSION

This paper presents a modified version of the link deficit algorithm which results in a lower cost starting network, when we desire to set up a $k$-connected network. In particular when $k=3$, a novel algorithm which utilizes the minimal spanning tree algorithm twice has been presented.

REFERENCES

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