



Performance Evaluation of Adaptive Line Enhancer Implementated with LMS, NLMS and BLMS Algorithm for Frequency Range 3-300Hz

Shobhit Agarwal¹, Raghu Raj Singh², Namrta Dadheech³, Sarita Chauhan⁴

B.Tech Student, Dept. of ECE, M.L.V Textile and Engineering College, Bhilwara, Rajasthan, India^{1,2,3}

Assistant Professor, Head of Dept. of ECE, M.L.V Textile and Engineering College, Bhilwara, Rajasthan, India⁴

ABSTRACT : In this paper, an adaptive line enhancer using LMS, BLMS and NLMS algorithm has been simulated for low electromagnetic frequency range (ELF & SLF-3 to 300 Hz.) range using MATLAB software. Firstly, sinusoidal wave is corrupted with the white noise then we have adaptively filtered corrupted wave over the required frequency range, but in the paper only 60 Hz result have been shown. Later on, the adaptive behaviour of the algorithms is analyzed and performance criteria are used in the study of these algorithms are: the minimum mean square error (MSE) and Signal to noise ratio. The paper compares a performances of ALE using LMS, NLMS and the BLMS algorithms for a given range. Different SNR ratio level is obtained as the step-size is changes, their relative SNR result is shown.

KEYWORDS: Adaptive Line Enhancer (ALE), Least Mean Square (LMS), Block LMS (BLMS), Normalised least mean square (NLMS), Extremely low frequency (ELF), Super low frequency (SLF), MSE (mean squared error)

I. INTRODUCTION

Adaptive filter is that it uses the filter parameters of a moment ago to automatically adjust the filter parameters of the present moment, to adapt to the statistical properties of unknown signal and noise, in order to achieve optimal filter. Adaptive algorithms based on the least mean square (LMS) algorithm, normalized least mean square (NLMS), and block least mean square (BLMS) processing algorithms are applied to the adaptive filter technology to the noise, and through the simulation results prove that its performance is usually much better than using fixed digital filter.

Most of the submarine communication uses the very low frequency i.e. electromagnetic waves in the ELF and SLF frequency ranges (3–300 Hz) can penetrate seawater to depths of hundreds of meters, allowing communication with submarines at their operating depths. Hence using, the concept ALE on the signals that are affected by white noise, received in submarine can be filtered easily.

II. LITERATURE SURVEY

Signal processing field has been made substantial contributions over the past thirty years. Due to the advances in digital circuit design, digital signal processing (DSP) systems have become attractive. Filtering application of DSP includes digital systems. A signal is processed by digital systems to control the information contained in the input signal. The Adaptive filters are acceptable in any unknown environment. The Adaptive filter is a powerful device for signal processing and control applications in time variation environment of input statistics. To reduce the signal corruption stimulated by predictable and unpredictable noise adaptive filters are used. Some applications such as identification, inverse modelling, prediction and interference cancellation are essential to explicate the problem of acoustic echo & noise cancellation and related issue. Researchers have developed various algorithms for active interference cancellation to obtain adaptive filter mainly LMS, NLMS and BLMS algorithm. Rate of convergence, misadjustment, numerical robustness, computational requirements and stability are the performance measures of adaptive algorithm. The ANC (adaptive noise cancellation) and the ALE are two adaptive filtering systems with similar mechanisms but slightly different filter designs. The original ANC uses two sensors to receive the target signal and noise separately, whereas the

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 4, April 2015

ALE uses only a single sensor to detect the target signal buried in noise, though it may use the same adaptive. The ALE is in fact a degenerated form of ANC, consisting of a single sensor and delay $z^{-\Delta}$ to produce a delayed version of $d(n)$, denoted by $x(n)$, which de-correlates the noise while leaving the target signal component correlated. Ideally, the output $y(n)$ of the adaptive filter in the ALE is an estimate of the noise-free input signal. Hence, the ALE capability to extract the periodic and stochastic components of a signal can also be known as an adaptive self-tuning filter (Widrow *et al.* 1985, Campbell *et al.* 2002). The ALE becomes an interesting application in noise reduction because of its simplicity and ease of implementation. However, to obtain the best performance in its computational process, the optimal approach is to execute ALE on a better convergence rate of adaptive algorithm with a less complex adaptive filter structure algorithm as the ANC.

Electromagnetic waves in the ELF and SLF frequency ranges (3–300 Hz) can penetrate seawater to depths of hundreds of meters, allowing communication with submarines at their operating depths. Building an ELF transmitter is a formidable challenge, as they have to work at incredibly long wavelengths. Due to the technical difficulty of building an ELF transmitter, the U.S., Russia and India are the only nations known to have constructed ELF communication facilities. Until it was dismantled in late September 2004, the American *Seafarer*, later called *Project ELF* system (76 Hz), consisted of two antennas, located at Clam Lake, Wisconsin (since 1977), and at Republic, Michigan, in the Upper Peninsula (since 1980). The Russian antenna (*ZEVs*, 82 Hz) is installed at the Kola Peninsula near Murmansk. It was noticed in the West in the early 1990s. The Indian Navy has an operational ELF communication facility at the INS Kattabomman naval base to communicate with its Arihant class and Akula class submarines.

III. ADAPTIVE LINE ENHANCER

Adaptive line enhancer (ALE) is used in many signal processing fields for its capability of tracking a signal of interest. The main advantage of it is that it does not require any reference signal to eliminate the noise signal.

Fig. 1, show the adaptive filter setup, where $s(k)$, $d(k)$ and $e(k)$ are the input, the desired and the output error signals, respectively. The vector $h(n)$ is the $M \times 1$ column vector of filter coefficient at time k , in such a way that the output of signal, $y(k)$, is good estimate of the desired signal, $d(k)$. This filter is an adaptive filter whose tap weights are controlled by an adaptive algorithm. Thus ALE refers to the case where a noisy signal, $x(k)$, consisting of a sinusoidal component and the requirement is to remove the noise part of the signal. As a result, the predictor can only make a prediction about the sinusoidal component and when adapted to minimize the instantaneous squared error output, $e(k)$, the line enhancer will be a filter optimized (the Wiener solution) or tuned to the sinusoidal component.

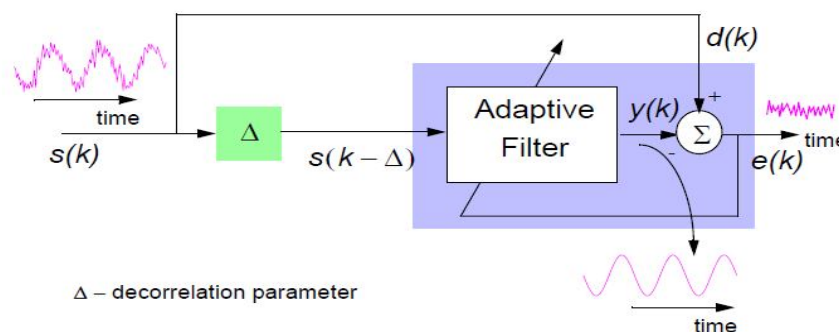


Figure.1-Basic Adaptive line enhancer

IV. ADAPTIVE ALGORITHM

1) Least Mean Square: The LMS algorithm which uses an instantaneous estimate of the gradient vector of a cost function is an approximation of the steepest descent algorithm. Based on sample values of the tap-input vector and an error signal the gradient is estimated. The algorithm iterates each coefficient in the filter, moving it in the direction of the



International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 4, April 2015

approximated gradient. For the LMS algorithm it is necessary to have a reference signal $d[n]$ representing the desired filter output. The difference between the reference signal and the actual output of the transversal filter is the error signal which is given in the equation (1)

$$y(n) = w^T(n)x(n) \text{ Filter Output(1)}$$

$$e(n) = d(n) - y(n) \text{ Error(2)}$$

$$w(n) = [w_0(n) \ w_1(n) \ \dots \ w_{M-1}(n)]^T \text{ Filter Coefficients at time } n \text{(3)}$$

$$x(n) = [x(n) \ x(n-1) \ x(n-2) \ \dots \ x(n-M+1)]^T \text{ Input Data(4)}$$

where the filter coefficients are calculated using the equation

$$w(n+1) = w(n) + 2\mu e(n)x(n) \text{(5)}$$

Considering as the step size (μ). The algorithm at each iteration requires that $x(n)$, $d(n)$ and $w(n)$ are known. As the step size decreases, the convergence speed to the optimal values is slower. This also implies that, the LMS algorithm is a stochastic gradient algorithm if the input signal is a stochastic process.

2)Block LMS:-In this method, the filter coefficients are held constant over each block of the input signal. The filter output $y(n)$ and error signal $e(n)$ are calculated using filter coefficients of that block. Then, the filter coefficients are updated at the end of each block using an average of the L gradient estimates over that block.

For k th block, the output of the filter is described as,

$$Y(kL + 1) = w_{kL}^T \cdot x(kL + 1) \dots \dots \dots (5)$$

and the error signal is given by,

$$e(kL + 1) = d(kL + 1) - y(kL + 1) \dots \dots \dots (6)$$

where, L is the block length and $d(n)$ is the desired signal.

The weight update equation of the k th block,

$$w_{(k+1)L} = w_{kL} + \mu/L \left(\sum_{l=0}^{L-1} e(kL + 1)x(kL + 1) \right) \dots (7)$$

3)Normalised LMS- The main drawback of the "pure" LMS algorithm is that it is sensitive to the scaling of its input. This makes it very hard to choose a learning rate μ that guarantees stability of the algorithm. The Normalised least mean squares (NLMS) filter is a variant of the LMS algorithm that solves this problem by normalising with the power of the input.

NLMS algorithm summary:

Parameters: P = filter order

μ = step size

Initialization: $\hat{h}(0) = 0$

Computation: For $n = 0, 1, 2, \dots$

$$X(n) = [x(n), x(n-1), \dots, x(n-p+1)]^T \dots \dots \dots (8)$$

$$e(n) = d(n) - \hat{h}^H(n)X(n) \dots \dots \dots (9)$$

$$\hat{h}(n+1) = \hat{h}(n) + \frac{\mu e^*(n)X(n)}{X^H(n)X(n)} \dots \dots \dots (10)$$

V. MEAN SQUARED ERROR

In this portion, we plot the error obtained from the equation 2,6 & 9. Firstly, error is squared and then, plotted with respect to simulation time and finally response obtained is smoothen. Smoothing is done by moving average filter that smoothes data by replacing each data point with the average of the neighboring data points defined within the span.

VI. RESULT AND DISCUSSION

In this section, adaptive line enhancer is designed with the help of three different algorithms i.e LMS, BLMS and NLMS. For the evaluation, firstly input signal is contaminated with white noise therefore, we have consider μ -noise equals to zero '0' and sigma noise to be '0.008'. Then a noisy weak signal is filtered by adaptive line enhancer designed by different algorithm. The result presented here with input signal of frequencies of 60Hz. The filtered output

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 4, April 2015

from different algorithms are shown in figure. Here Filtered signal is of 60Hz (Shown in fig.2,3,4) The order of the filter was set to $M=16$. Similarly, signal at other frequency can also be filtered and will produce same SNR ratio, since change in frequency doesn't alter the power of signal.

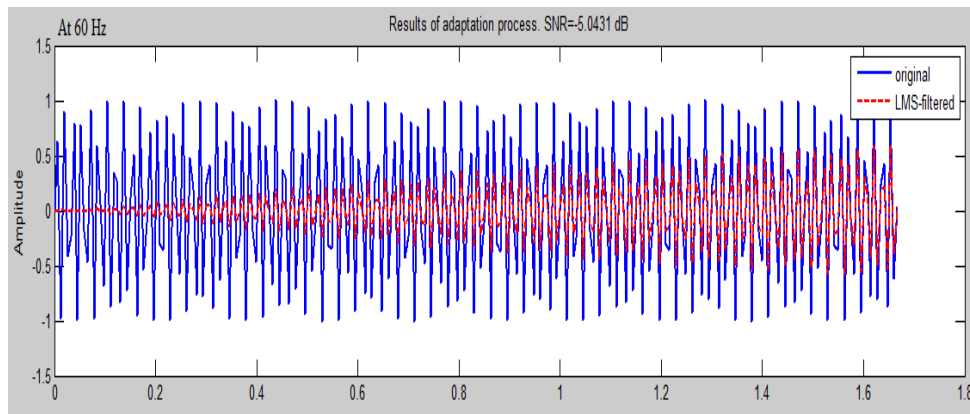


Fig. 2 LMS filtered output at 60hz Blue colour wave represent original signal and red colour wave shows LMS filtered output

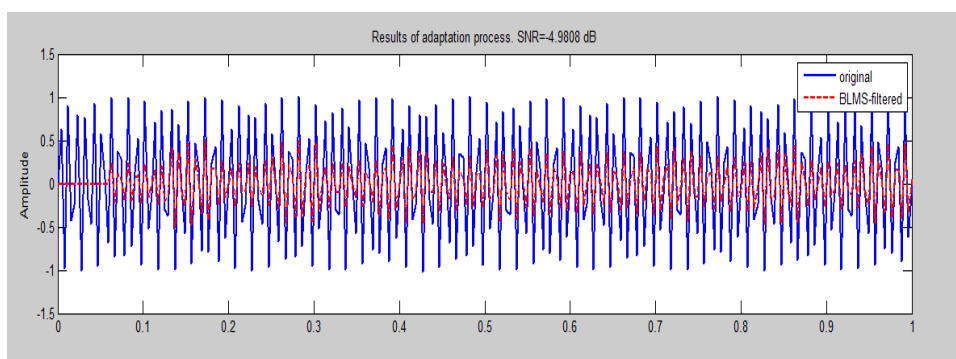


Fig. 3 BLMS filtered signal at 60hz. Blue colour wave represent original signal and red colour wave shows BLMS filtered output

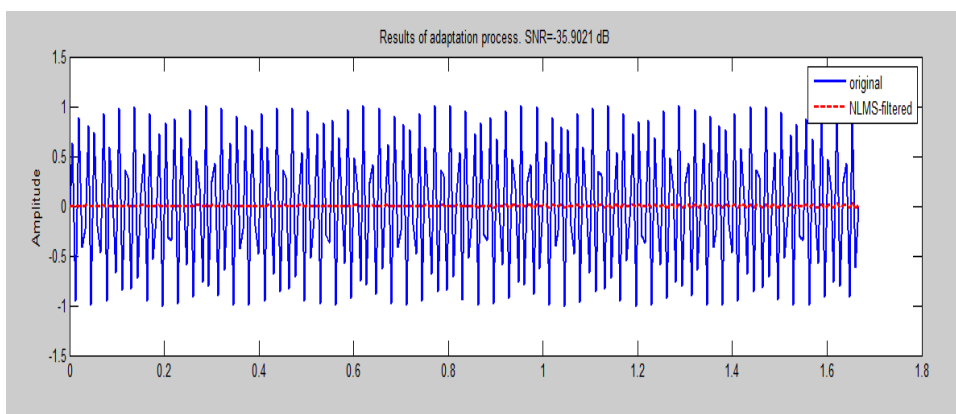


Fig4:NLMS filtered signal at 60 Hz. Blue colour wave represent original signal and red colour wave shows NLMS filtered output

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 4, April 2015

Secondly, we change the value of step-size or convergence factor and then observe the change in SNR values of filtered output, as equations 1, 5 & 9. Choosing the step size is completely a hit trail method. Below given table shows the value of SNR obtained at different stepsize

S.No	StepSize	LMS	NLMS	BLMS
1	0.001	-2.522	-20.354	-12.41
2	0.002	0.379	-17.337	-9.404
3	0.003	1.872	-15.568	-7.658
4	0.004	2.776	-14.313	-6.436
5	0.005	3.390	-13.331	-5.472
6	0.006	3.852	-12.532	-4.692
7	0.007	4.192	-11.854	-4.019
8	0.008	4.468	-11.267	-3.445
9	0.009	4.695	-10.757	-2.952
10	0.010	4.895	-10.285	-2.494

Table1-SNR obtained at different step-size for LMS,NLMS,BLMS

In Table 1, negative value represent, that power of error signal is greater than information signal. This is possible since input signal is of low frequency.

Given below graph represent squared error graph at the step size of 0.01 with respect to simulation time.

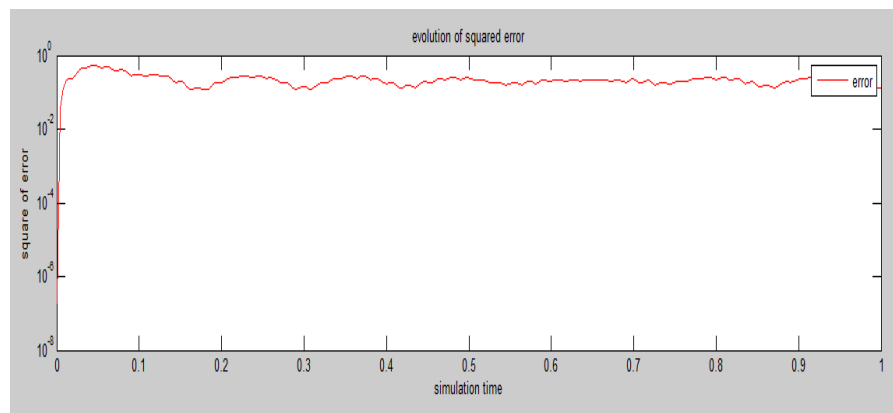


Fig.5-BLMS mean squared error

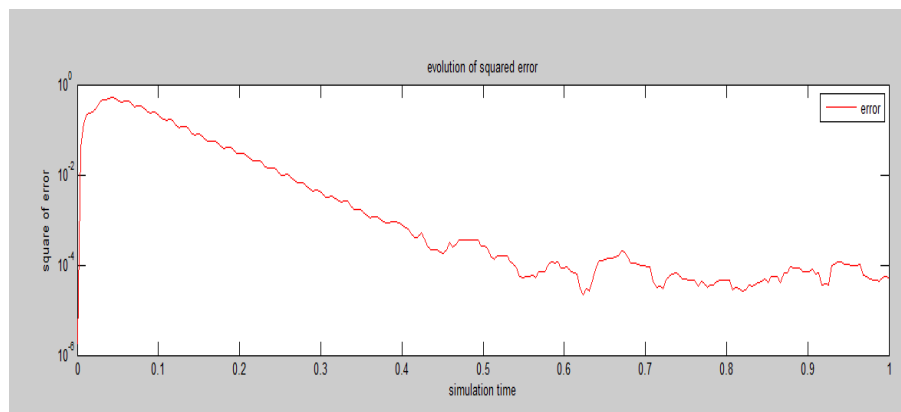


Fig.6-LMS mean squared error

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 4, April 2015

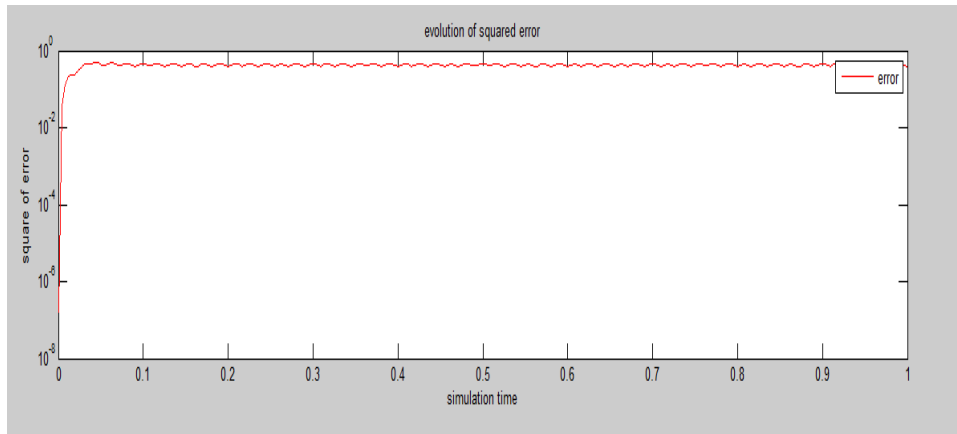


Fig.7-NLMS squared mean error

From Square mean(Fig.5,6,7)error plot we can say that error is quite near to zero and the constant error corresponds that the system is converging. In addition to the algorithm, the step size and filter length of an adaptive filter also affect the convergence speed. The learning curve of an adaptive filter gradually converges to zero and becomes steady at an MSE value of the error signal $e(n)$. The difference between that MSE value and zero is known as the steady state error. An optimal adaptive filter typically has a small steady state error. You can minimize the steady state error by adjusting the step size and filter length of the adaptive filter

VI.CONCLUSION

For the low EMW(3-300hz), we can conclude that NLMS's performance is much better than LMS and BLMS. If we consider the table then at step size 0.007 we can obtain best result for all the algorithm. SNR is highly dependent on the step size so, we have to choose such that it produces good result and even take less convergence time.

REFERENCES

- [1] S. Arunkumar, P. Parthiban, S. Aravind Kumar-Implementation Of Least Mean Square Algorithm For Sinusoidal And Audio Denoising Using Fpga-Vol. 2, Issue 12, December 2013
- [2] K. Prameela, M. Ajay Kumar, Mohammad Zia-Ur-Rahman and Dr B V Rama Mohana Rao-Non Stationary Noise Removal from Speech Signals using Variable Step Size Strategy
- [3] Simon Haykin, "Adaptive Filter Theory", Prentice Hall, 1996
- [4] "Navy gets new facility to communicate with nuclear submarines prowling underwater". The Times of India 31 July 2014.
- [5] Yuu-Seng Lau, Zahir M. Hussian and Richard Harris, "Performance of Adaptive Filtering Algorithms: A Comparative Study", Australian Telecommunications, Networks and Applications Conference (ATNAC), Melbourne, 2003.
- [6] Manoj Sharma "Acoustic Echo Reduction Using Adaptive Filter: A Literature Review", MIT International Journal of Electrical and Instrumentation Engineering, Vol. 4, No. 1, January 2014, pp. 7-11 ISSN 2230-7656 © MIT Publications
- [7] Ying He, *et. al.* "The Applications and Simulation of Adaptive Filter in Noise Canceling", 2008 international Conference on Computer Science and Software Engineering, 2008, Vol.4, Page(s): 1 - 4.
- [8] Sen M. Kuo, Sohini Mitra and Woon-Seng Gan, "Adaptive Feedback Active Noise Control Headset: Implementation, Evaluation and Its Extensions" IEEE Transactions on Control Systems Technology, Vol. 14, No.2, March 2006