



Improved Diversity Analysis of Coded OFDM in Frequency Selective Channels

Koshy G¹, Soumya J. W²

PG Scholar (Communication Engineering), Dept. of ECE, CAARMEL Engineering College, Mahatma Gandhi
University, Kerala, India¹

Assistant Professor, Dept. of ECE, CAARMEL Engineering College, Mahatma Gandhi University, Kerala, India²

ABSTRACT: For broadband wireless communication systems, Multi-Input Multi-Output (MIMO) techniques have been incorporated with Orthogonal Frequency Division Multiplexing (OFDM). Beamforming is a multi-input multi-output technique utilizing the channel knowledge both at the transmitter and the receiver. Multiple beamforming uses more than one subchannel to improve the capacity. For frequency selective channels, to achieve Inter Symbol Interference and achieve spatial diversity combine beamforming with OFDM. Also by adding channel coding spatial diversity and multipath diversity can be achieved. The diversity analysis of BICMB-OFDM-SG is limited to $R_c SL \leq 1$ where L is the number of channel taps, S is the number of parallel streams transmitted at each subcarrier and R_c is the code rate. In this paper precoding technique is employed to overcome this limitation. Also precoding provides better performance. Also LDPC coding techniques is introduced for improved diversity.

KEYWORDS: MIMO systems, Beamforming, diversity methods, subcarrier multiplexing.

I. INTRODUCTION

High spectral efficiency and performance for a given bandwidth can be achieved by Multiple-Input Multiple-Output (MIMO) systems. In flat fading MIMO channels, single beamforming carrying only one symbol at a time achieves full diversity but spatial multiplexing without channel coding results in the loss of the full diversity order. Bit-Interleaved Coded Multiple Beamforming (BICMB) overcomes the performance degradation.

If the channel is in frequency selective fading, Orthogonal Frequency Division Multiplexing (OFDM) can be used to combat the Inter-Symbol Interference (ISI) caused by multipath propagation. Along with this for MIMO channels beamforming achieves multipath diversity and spatial diversity. Advantage of OFDM is that it has high spectral efficiency. By adding channel coding multipath diversity can be achieved. Both spatial diversity and multipath diversity can be achieved by adding channel coding. The subcarrier grouping technique is employed to provide multi-user compatibility. Bit-Interleaved Coded Multiple Beamforming Orthogonal Frequency Division Multiplexing with Subcarrier Grouping (BICMB-OFDM-SG) technique exploits these properties. For broadband wireless communication BICMB-OFDM be an important technique. In this paper, the diversity analysis of BICMB-OFDM-SG with precoding is carried out.

II. RELATED WORK

Multiple antennas can be used for increasing the amount of diversity or the number of degrees of freedom in wireless communication systems [1]. Single and multiple beamforming can be used to exploit the perfect channel state information (CSI) available both at the transmitter and the receiver of a multi-antenna wireless system [3]. The average and outage performance of spatial multiplexing multiple-input multiple-output (MIMO) systems with channel state information at both sides of the link is analysed in [4]. Achieving full spatial multiplexing and full diversity in wireless communications suggested that using multiple antennas provides a substantial capacity and diversity increase for wireless communication systems. A multi-input multi-output (MIMO) technique that utilizes the channel knowledge both at the transmitter and the receiver is known as Beamforming [5]. If the channel is frequency selective, then BICMB is combined with orthogonal frequency division multiplexing (OFDM) (BICMB-OFDM) in order to combat ISI caused

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 8, August 2015

by the frequency-selective channels[6].Designed a bit interleaved coded modulations including a partial algebraic precoder in order to transmit several spatial streams with full diversity over a transmit beamformed MIMO channel[7]. Orthogonal frequency division multiplexing (OFDM) has been shown to get ISI very well by converting the frequency selective channel into parallel at fading channels [9].The combination of bit interleaved coded modulation (BICM) and OFDM achieves the full frequency diversity ordered by a frequency selective channel with any kind of power delay profile [10].The use of channel knowledge at the transmitter, the technique known as beamforming, achieves the maximum diversity in space when the best Eigenmode is used (single beamforming)[11].

II. SYSTEM MODEL

Consider a BICMB-OFDM-SG system employing N_t transmit and N_r receive antennas, a convolutional code of code rate R_c , and transmitting S parallel data streams.

First, generate the binary message and it is encoded using convolution encoder of code rate R_c . Trellis Structure is used to create required code rate, for a high rate punctured code a perforation matrix is combined. From the information bits this generates the bit codeword c . The code word is given to bit interleaver. For burst error-correction, interleaving is widely used. Here random bit interleaver is used.

In digital communication and storage systems, to improve the performance of forward error correcting codes interleaving is used frequently. Many communication channels in now a days are not memoryless. So errors typically occur in bursts rather than independently. It fails to recover the original code word, if the number of errors within a code word exceeds the error-correcting code's capability. Interleaving creates a more uniform distribution of errors by shuffling source symbols across several code words. Interleaving in multi carrier communication also provide frequency diversity e.g., to mitigate frequency-selective fading or narrowband interference.

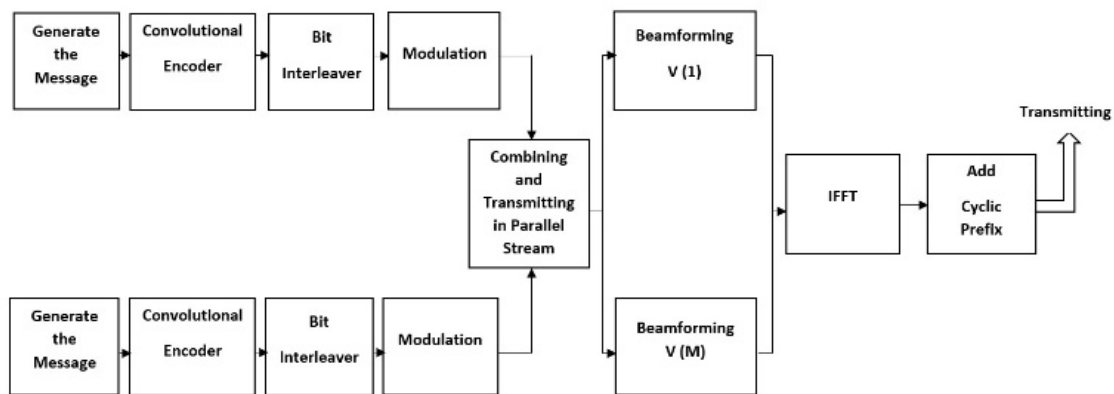


Fig. 1: Bit Interleaved Coded Multiple Beamforming with Subcarrier Grouping transmitter side

The interleaved bit sequence is then modulated, here Quadrature Amplitude Modulation (QAM) is used. Let the number of streams transmitted for each subcarrier be $S \leq \min\{N_t, N_r\}$ where N_t and N_r be the number of transmit and receive antennas. The symbol sequence is transmitted through M subcarriers. Hence, an $S \times 1$ symbol vector $x_k(m)$ is transmitted through the m^{th} subcarrier at the k^{th} time instant with $m = 1, \dots, M$. Inverse Fourier Transform is applied to the sequence. Then Cyclic Prefix is added to the sequence. The length of Cyclic Prefix (CP) is $L_{cp} \geq L$ with L denoting the number of channel taps. Cyclic prefix is employed by OFDM to combat ISI caused by multipath propagation. It is then transmitted.

Let the quasi-static flat fading MIMO channel observed at the m^{th} subcarrier be $H(m)$. The frequency selective fading MIMO channel is assumed to be Rayleigh fading channel. For each subcarrier the Singular Value Decomposition beamforming is carried out. The beamforming matrices at the m^{th} subcarrier are determined by SVD of $H(m)$,

$$H(m) = U(m)\Lambda(m)V^H(m),$$

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 8, August 2015

where the $U(m)$ matrix has order of $N_r \times N_r$ and the $V(m)$ matrix of $N_t \times N_t$ are unitary, and the $N_r \times N_t$ matrix $\Lambda(m)$ is diagonal rectangular matrix. When S streams are transmitted at the same time, $U(m)$ and $V(m)$ are chosen as beamforming matrices at the receiver and transmitter at their m^{th} subcarrier, respectively. The multiplications with beamforming matrices are carried out for each subcarrier.

The system input-output relation for the m^{th} subcarrier at the k^{th} time instant is

$$y_{k,s}(m) = \lambda_s(m)x_{k,s}(m) + n_{k,s}(m)$$

with $s = 1, \dots, S$, where $y_{k,s}(m)$ and $x_{k,s}(m)$ are the s^{th} element of the $S \times 1$ received symbol vector $y_k(m)$ and the transmitted symbol vector $x_k(m)$ respectively, and $n_{k,s}(m)$ is the additive white Gaussian noise with zero mean.

In the receiver side the received data contains added white noise. Cyclic prefix is being removed from the received data. Then Fourier transform is applied to the sequence. Using the Beamforming matrix $U(m)$, information is retrieved. The data is then separated to different encoders. Each encoding section consists of QAM demodulator, Random Bit De-interleaver, and Viterbi decoder. The output obtained from the decoder is the recreated message.

Finally, the Viterbi decoder, which applies the soft-input Viterbi decoding to find the information bit sequence \hat{b} the message from the codeword \hat{c} with the minimum sum weight.

The Maximum Likelihood (ML) bit metrics at the receiver for $c_k = b \in \{0, 1\}$ as

$$\Delta(y_{k,s}(m), c_{k'}) = \min_{x \in X_{c_{k'}}} |y_{k,s}(m) - \lambda_s(m)x|^2$$

and makes decisions according to

$$\hat{c} = \arg \min_c \sum_{k'} \Delta(y_{k,s}(m), c_{k'})$$

In the receiver side the received data contains added white noise. Cyclic prefix is being removed from the received data. Then Fourier transform is applied to the sequence. Using the Beamforming matrix $U(m)$, information is retrieved. The data is then separated to different encoders. Each encoding section consists of QAM demodulator, Random Bit De-interleaver, and Viterbi decoder. The output obtained from the decoder is the recreated message.

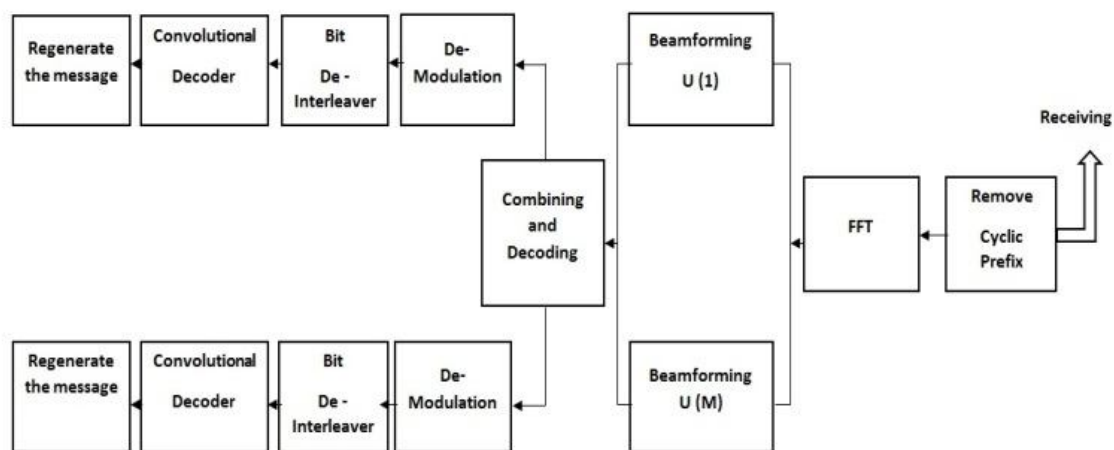


Fig. 2: Bit Interleaved Coded Multiple Beamforming with Subcarrier Grouping receiver side

Finally, the Viterbi decoder, which applies the soft-input Viterbi decoding to find the information bit sequence \hat{b} the message from the codeword \hat{c} with the minimum sum weight.

The Maximum Likelihood (ML) bit metrics at the receiver for $c_k = b \in \{0, 1\}$ as

$$\Delta(y_{k,s}(m), c_{k'}) = \min_{x \in X_{c_{k'}}} |y_{k,s}(m) - \lambda_s(m)x|^2$$

and makes decisions according to

$$\hat{c} = \arg \min_c \sum_{k'} \Delta(y_{k,s}(m), c_{k'})$$

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 8, August 2015

In practice, number of subcarriers M is always much larger than number of taps L . There exists correlation among subcarriers. Due to subcarrier correlation it will cause performance degradation. Subcarrier grouping is done to overcome the performance degradation. The subcarrier grouping technique is to transmit information through multiple group of subcarriers through multiple streams. The advantages of using OFDM are multi-user interference elimination, complexity reduction and Peak-to-Average Ratio (PAR) reduction.

For $L < M$, although there exists among subcarriers some subcarriers could be uncorrelated numbers. There are $G = M/L$ groups of uncorrelated subcarriers. So transmit multiple streams of bit codewords through these G different groups of uncorrelated subcarriers

The diversity of BIMB-OFDM_SG is limited to $R_cSL \leq 1$. In the case of $R_cSL > 1$, there always exists at least an error path with no errored bits transmitted through the first subchannel of a subcarrier. Proof of the limitation is explained in [2].

III. PROPOSED METHOD

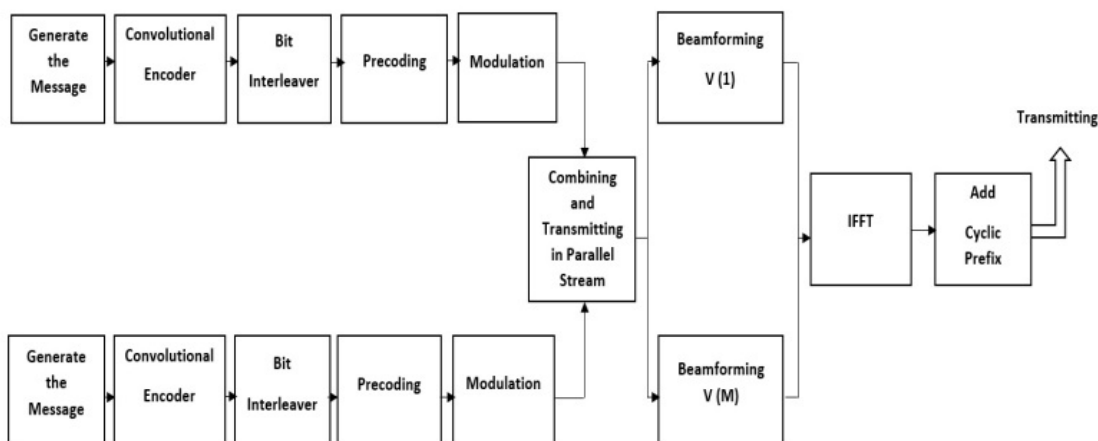


Fig.3: BICMB-OFDM_SG with precoding transmitter side

The precoding technique can be applied to each subcarrier. As compared to BICMBOFDM-SG in Fig. 1, two more precoding blocks are added along with the channel coding, bit interleaver, and modulation. At the receiver side post decoding is done. Using this precoding technique it is able to overcome the criteria BICMB-OFDM-SG of $R_cSL \leq 1$. So it provides better performance with the same transmission rate and offers multi-user compatibility.

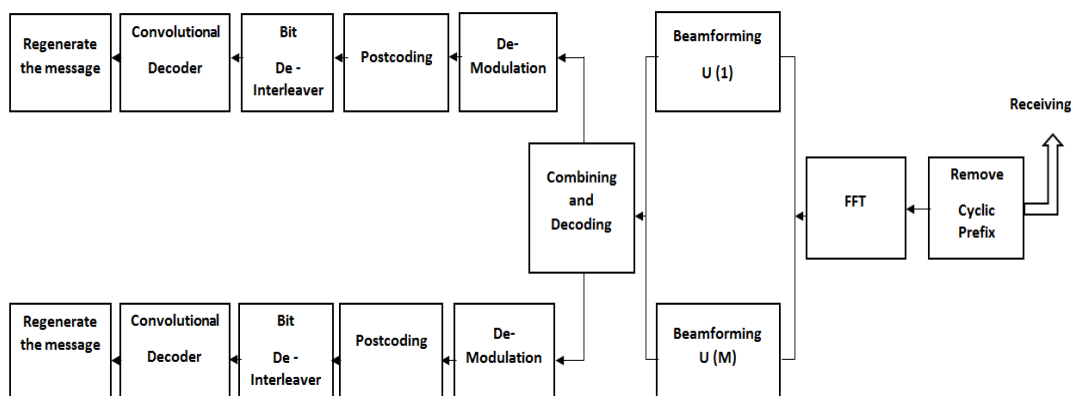


Fig. 4: BICMB-OFDM_SG with precoding receiver side

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 8, August 2015

Fig. 3 and fig. 4 represents the structure of BICMB-OFDM-SG with precoding. In MIMO antenna communications precoding is a generalization of beamforming to support multi-stream transmission.

In precoding data from the interleaver is being previously coded before transmitting. The precoded data is then combined, beamformed and transmitted. At the receiving side after receiving the data, the postcoding technique is done. Information obtained after postcoding is given to demodulator, deinterleaver and decoder.

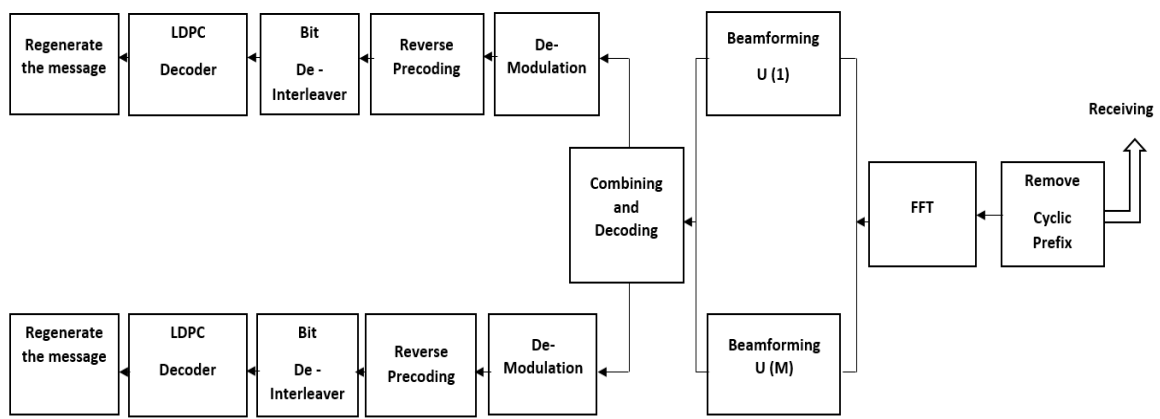


Fig.5: Improved BICMB-OFDM-SG transmitter side

For further improvement convolutional coding scheme is replaced low-density parity-check (LDPC) code. LDPC coding scheme has many advantages over convolutional codes. LDPC is a linear error correcting code. LDPC enables the transmission of a message over a noisy transmission. LDPC achieves shanon limit, so these codes are called as capacity-approaching codes. Probability of lost information is very less. Figure 5 and 6 shows the transmitter and receiver of improved BICMB-OFDM-SG.

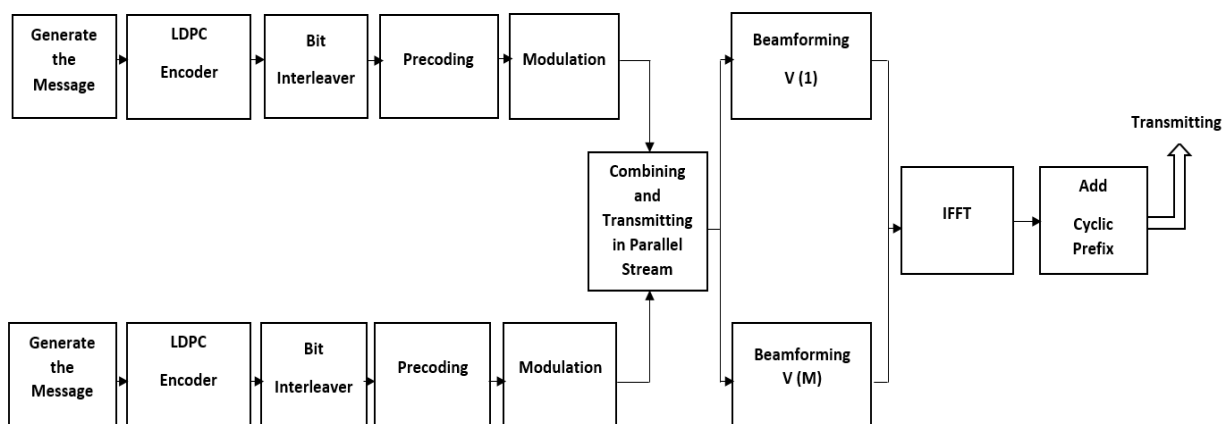


Fig.6: Improved BICMB-OFDM-SG receiver side

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 8, August 2015

IV. SIMULATION RESULTS

The simulation is done on MATLAB 2010. To verify the diversity analysis, using these values with number of taps $L = 1$, number of subcarriers $M = 64$ using 16-QAM are considered for simulations. The number of employed subchannels for each subcarrier is assumed to be the same. The generator polynomials in octal for the convolutional codes with $R_c = 1/2$ is (5, 7) respectively. The length of CP is $L_{cp} = 8$. Number of parallel streams are $S=1$ and $S=2$ is being considered.

For improved BICMB-OFDM-SG there requires creation of parity sparse matrix. The parity matrix used is of the order 4096×12288 with number of information bit $n = 4096$ and number of encoded bits $k = 8192$.

The figure 1 and 2 shows the existing system of BICMB-OFDM-SG transmitting side and receiving side. Figure 3 and 4 shows the BICMB-OFDM-SG with precoding transmitting side and receiving side. Figure 7 shows the BER vs. SNR for BICMB-OFDM-SG with and without precoding over equal power channel taps.

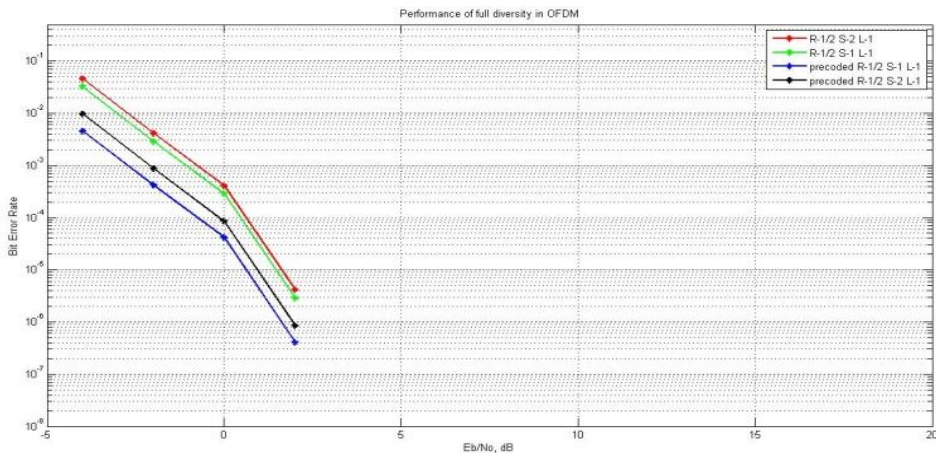


Fig.7: BER vs. SNR for BICMB-OFDM-SG with and without precoding over equal power channel taps.

Figure 5 and 6 shows the Improved BICMB-OFDM-SG with precoding transmitting side and receiving side. Figure 7 shows the BER vs. SNR for BICMB-OFDM-SG for Convolutional codes and LDPC over equal power channel taps.

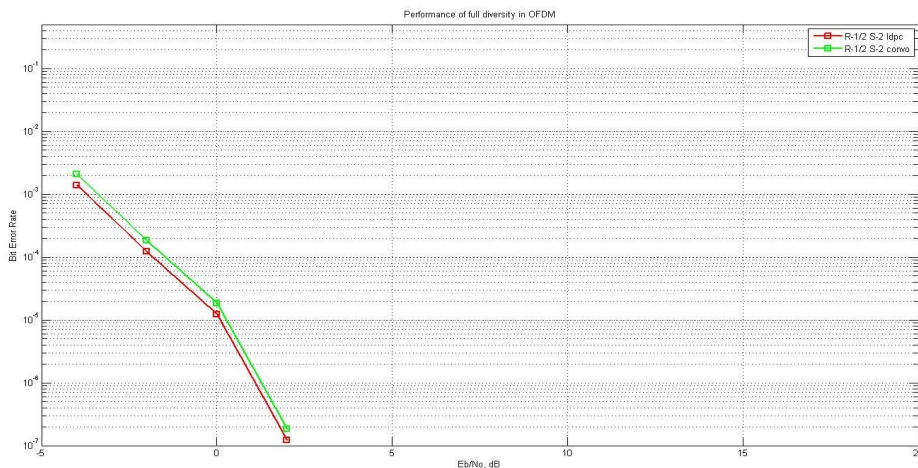


Fig.8: BER vs. SNR for BICMB-OFDM-SG for Convolutional codes and LDPC



International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 8, August 2015

V. CONCLUSION

For frequency selective fading MIMO channels BICMB-OFDM_SG combines MIMO and OFDM to achieve spatial diversity, multipath diversity, spatial multiplexing, and frequency multiplexing. For broadband wireless communication it is an important technique. The comparison of BICMB-OFDM-SG and BICMB-OFDM-SG with precoding is carried out in this paper.

A sufficient and necessary condition in BICMB-OFDM-SG for achieving full diversity was $R_c SL \leq 1$. So using this precoding technique it is able to overcome the limitation and provides better result. Precoding also provides multi-user compatibility. So it is a very important technique in practical application. Further improvement in diversity analysis can be done by using Turbo Codes instead of LDPC.

REFERENCES

- [1] L. Zheng and D. Tse, "Diversity and multiplexing: a fundamental tradeoff in multiple-antenna channels", IEEE Trans. Inf. Theory, Vol.49, No.5, pp.1073-1096, May 2003.
- [2] Boyu Li and Ender Ayanoglu, "Diversity Analysis of Bit-Interleaved Coded Multiple Beamforming with Orthogonal Frequency Division Multiplexing", IEEE Trans. Communications, Vol.61, No.9, September 2013.
- [3] E. Sengul, E. Akay and E. Ayanoglu, "Diversity analysis of single and multiple beamforming", IEEE Trans. Commun., Vol.54, No.6, pp.990-993, June 2006.
- [4] L. G. Ordoez, D. P. Palomar, A. Pages-Zamora and J. R. Fonollosa, "High-SNR analytical performance of spatial multiplexing MIMO systems with CSI", IEEE Trans. Signal Process., Vol.55, No.11, pp.5447-5463, November 2007.
- [5] E. Akay, E. Sengul and E. Ayanoglu, "Achieving full spatial multiplexing and full diversity in wireless communications", IEEE WCNC, pp.2046-2050, 2006.
- [6] Enis Akay, Ersin Sengul and Ender Ayanoglu "Bit-interleaved coded multiple Beamforming", IEEE Trans. Commun., Vol.55, No.9, pp.1802-1811, Sep. 2007.
- [7] N. Gresset and M. Khanfouci, "Precoded BICM design for MIMO transmit beamforming and associated low-complexity algebraic receivers", IEEE GLOBECOM, 2008.
- [8] H. J. Park and E. Ayanoglu, "Diversity analysis of bit-interleaved coded multiple Beamforming", IEEE ICC, 2009.
- [9] Enis Akay and Ender Ayanoglu, "Full Frequency Diversity Codes for Single Input Single Output Systems", IEEE VTC Fall, Vol.3, pp.1870-1874, 2004.
- [10] Enis Akay and Ender Ayanoglu, "Achieving Full Frequency and Space Diversity in Wireless Systems via BICM, OFDM, STBC and Viterbi Decoding", IEEE Trans. Commun., Vol.54, No. 2, pp.2164-2172, Dec. 2006.
- [11] E. Akay, E. Sengul and E. Ayanoglu, "Performance analysis of beamforming for MIMO OFDM with BICM", IEEE ICC, Vol.1, pp.613-617, 2005.
- [12] Z. Wang and G. B. Giannakis, "Wireless multicarrier communications: where Fourier meets Shannon", IEEE Signal Process. Mag., Vol. 17, No. 3, pp.29-48, May 2000.
- [13] D. L. Goeckel and G. Ananthaswamy, "On the design of multidimensional signal sets for OFDM systems", IEEE Trans. Commun., Vol.50, No.3, pp.442-452, Mar. 2002.
- [14] Z. Liu, Y. Xin, and G. B. Giannakis, "Linear constellation precoding for OFDM with maximum multipath diversity and coding gains", IEEE Trans. Commun., Vol.51, No.3, pp.416-427, Mar. 2003.
- [15] D. Haccoun and G. Begin, "High-rate punctured convolutional codes for Viterbi and sequential decoding", IEEE Trans. Commun., Vol.37, No.11, pp. 1113-1125, Nov. 1989.
- [16] I. Lee, A. M. Chan, and C.-E. W. Sundberg, "Space-time bit-interleaved coded modulation for OFDM systems", IEEE Trans. Signal Process., Vol.52, No.3, pp.820-825, Mar. 2004.
- [17] Z. Liu, Y. Xin, and G. B. Giannakis, "Space-time-frequency coded OFDM over frequency-selective fading channels", IEEE Trans. Signal Process., Vol.50, No.10, pp.2465-2476, Oct. 2002.