Analysis and Design of Controller for PWM Rectifiers

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ABSTRACT: The primary application of rectifiers is to derive DC power from an AC supply. Virtually all electronic devices require DC, so rectifiers are used inside the power supplies of all electronic equipment. PWM rectifier is now becoming popular due to its low distortion input current, unity power factor operation, bi-directional power flow ability and can offer excellent dynamic response of the dc output voltage. A three-phase PWM rectifier used together with closed-loop dc–dc converters for converting DC power from one voltage to another is much more complicated. In order to perform the above operation rectifier switches should be controlled properly. Hence it is much needed to design a suitable controller for single phase and three phase rectifier. From the small signal transfer function model, the controllers can be designed. The modelling of single phase, three phase rectifiers and suitable controller design for the modelled rectifier circuit and the simulated results are presented.

KEYWORDS: Single phase rectifiers, mathematical model, bidirectional AC-DC converters.

I.INTRODUCTION

The single-phase voltage source PWM rectifier (VSR) is widely used in improving the quality of the power energy. Recently, lots of researches have been investigated for the Single-Phase PWM rectifier. The single-phase PWM rectifier is now becoming more and more popular due to its low distortion input current, unity power factor operation and bi-directional power flow ability. As the filter capacitor required is generally small under balanced supply voltage conditions, it may also be believed that these converters can offer excellent dynamic response of the dc output voltage.
In general, the selection of an appropriate controller of a PWM rectifier in consideration of stability and dynamic performances requires good knowledge about the characteristics of the system to be controlled. Various strategies have been applied on the single-phase PWM rectifier, such as states-space averaging and circuit methods.

A three-phase PWM rectifier is often used together with closed-loop dc–dc converters as loads. The three phase PWM rectifier can be compared with the working of DC-DC boost converter. SISO model can be derived for the three phase PWM rectifier so that it can be comparable with the DC-DC boost converter. In this paper, the suitable controller for small signal transfer function model for single phase PWM rectifier was designed under closed loop operation and also SISO model, controller for closed loop operation of three phase rectifier was designed.

II.BOOST RECTIFIER

Single-phase PWM rectifier based on the small signal model are dealt in detail. The purpose is to decrease the voltage fluctuations and increase the dynamic performance of the rectifier when the load changes suddenly. The procedure for deriving the transfer function are to make assumptions then define the state variables and write state equations for each interval of operation, average the state equations over a switching cycle and introduce perturbation in state variables then equate ac and dc quantities and proceed with ac equations and take Laplace transform, prepare matrix Small signal model and calculate desired transfer functions

The fig.1. shows the basic equivalent circuit of single phase PWM rectifier. Fig.2. and Fig.3 shows the mode of operation for PWM rectifier acting as a boost rectifier. PWM rectifier can be used as bidirectional rectifiers. Rectifier operation is performed by the diodes, while the inverter operation is performed by switches. As tabulated in table 1, it can operate the rectifier in a boost mode by controlling the switches T_1, T_2 with the help of the inductor at source.
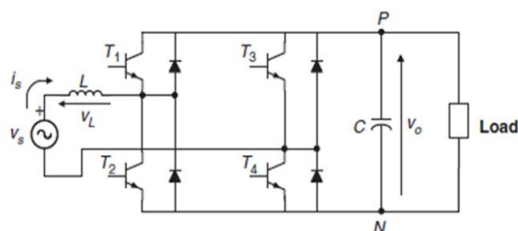
Fig. 1 Single phase Boost rectifier

Under steady state operation, mode 1, when switch T_2 is ON, the conduction path is given by V_S-L-T_2-D_4. Hence the inductor is charging, since there is no connection to the load. This mode of operation is similar to that of the DC-DC boost converter operation when switch is ON. In Mode 2, when T_2 is OFF, the conduction path will be V_S-L-D_1-load-D_4. Here the inductor is discharing mode. More over the switches T_3 and T_4 has no effect on the operation of a boost rectifier.
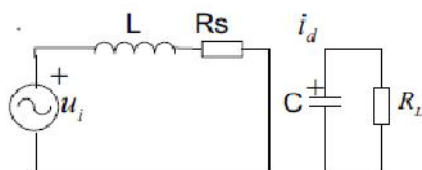
Fig. 2 Mode 1/3 operation   Fig.3 Mode 2/4 operation
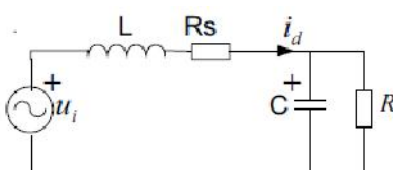
TABLE I. MODES OF OPERATION   .

SUPPLY	MODE	T_1	T_2	PATH
$+_{ve}$ cycle	1	OFF	ON	V_S-L-T_2-D_4
$+_{ve}$ cycle	2	ON	OFF	V_S-L-D_1-l-D_4
$-_{ve}$ cycle	3	ON	OFF	V_S-D_3-T_1-L
$-_{ve}$ cycle	4	OFF	ON	V_S-D_3-l-D_2-L

III. DESIGN OF CONVERTER PARAMETERS

Inductor and capacitor will play a major role in the boost rectifier as shown in the operation. Inductance is used for bi-directional power flow and boost operation, while the capacitance is used to maintain the constant DC output for a period of time by reduce the output DC ripples. Hence designing of inductance and capacitance have a significant role in the operation. Moreover the modulating index must be less than 1 for PWM pulse. Hence the amplitude of modulating signal must be greater than of the amplitude of carrier signal.

A. VOLTAGE GAIN:

The boost voltage obtained in the output can be calculated by
$$V_o = V_s * M.I/(1-d) \qquad (1)$$
Where, M.I = Modulating index
d = switching period

B. INDUCTANCE:

The fundamental component of PWM switch should be given by V_r. It should be varied from the supply voltage at an angle of δ as the line is similar to that of transmission line.
The inductance can be derived as follows
V_r=Fundamental component of PWM waveform
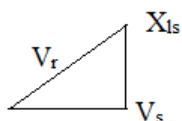V_s= Supply Voltage, I_s= Supply currents

Fig.4.Phasor diagram

$V_r = \sqrt{(V_s{}^\wedge 2 + (L\omega I_s)^\wedge 2)}$ (2)
From the above equation we can find L as
$L = \sqrt{((V_r{}^2 - V_s{}^2)/\omega^2 I_s{}^2)}$ (3)

*C.*CAPACITANCE:

I_L, the load current contains DC current and ripple current. Capacitor makes I_L perfect DC and ripple should be maximum of 5%. By equating output power equals to input power and equate I_L with the AC part we can obtain the value of capacitance as follows
$C \geq (MI * I_s)/(4\omega\Delta V)$ (4)

*D.*CARRIER FREQUENCY:

The carrier frequency should be minimum in the order of $11 * f_s$, where f_s is the supply or fundamental frequency. For 50Hz supply it should be above 550Hz. Most probably 2KHz is chosen.

IV. SMALL SIGNAL MODEL

Assume all of the switches are ideal time-variant switch model. Also, suppose the inductor current and the capacitor voltage is state variable. Then we can get the math model when the switches turn on/off. The mathematical model can be calculated as

$$L\frac{di}{dt} = u_i - u_c \qquad C\frac{du_c}{dt} = i - \frac{u_c}{R} \qquad (5)$$
$$L\frac{di}{dt} = u_i \qquad C\frac{du_c}{dt} = \frac{u_c}{R} \qquad (6)$$

So the following equations show the ideal small signal model

$$x = \begin{vmatrix} i \\ u_c \end{vmatrix}, \quad A_1 = \begin{bmatrix} 0 & 0 \\ 0 & 1/RC \end{bmatrix},$$

$$A_2 = \begin{bmatrix} 0 & 1/L \\ 1/C & -1/RC \end{bmatrix} \qquad B_1 = B_2 = \begin{bmatrix} 1/L \\ 0 \end{bmatrix}, \quad u = [u_i]$$

A.   AVERAGE STATE EQUATION:

The first step is to use the average state function instead of the two partition state functions. According to the proportion weighted average of the state function in on/off state, we get the state space average model in on switchperiod. Assume D is the average of the switch variable

$$\begin{cases} L\,di/dt = u_i - (1-D)u_c \\ C\,du_c/dt = (1-D)i + (2D-1)\,u_c/R \end{cases} \qquad (7)$$

The state-space average mode can be depicted as that

$$\begin{bmatrix} di/dt \\ du_c/dt \end{bmatrix} = \begin{bmatrix} 0 & -(1-D)/L \\ (1-D)/C(2D-1) & C(2D-1)/RC \end{bmatrix} \qquad (8)$$

$$y(t) = (DC_1 + (1-D)C_2)\begin{bmatrix} i \\ u_c \end{bmatrix} \qquad (9)$$

B. PERTURB AND LINEARIZATION

We know that low frequency and small ripple characteristic of the rectifier is satisfied, so the derivative of state vector in stable state equals to zero. According to that, we obtain that

$$X = -A^{-1}BU \qquad (10)$$

$$A = DA_1 + (1-D)A_2, \qquad B = DB_1 + (1-D)B_2$$

Assume the small disturbance arises,

$$x = X + \hat{x}, \; y = Y + \hat{y}, \quad u = U + \hat{u}, \; d = D + \hat{d} \qquad (11)$$

$$\hat{x}(t) = A\hat{x}(t) + B\hat{u}(t) + [(A_1 - A_2)X + (B_1 - B_2)U]\hat{d}(t)$$

$$\begin{cases} s\hat{x}(s) = A\hat{x}(s) + B\hat{u}(s) + [(A_1 - A_2)X + (B_1 - B_2)U_s]\hat{d}(s) \\ \qquad\qquad \hat{Y}(s) = C\hat{x}(s) \end{cases}$$

C. TRANSFER FUNCTION:

So we get the transfer function of state variable and output variable expressed as

$$G_i(s) = \frac{\hat{\imath}}{\hat{u}_i} = \frac{1}{s^2 + \frac{s}{(RC)} + (1-D)^2\Big/LC} * \left(\frac{s}{L} + \frac{1}{LRC}\right) \qquad (12)$$

$$G_u(s) = \frac{\hat{u}_c}{\hat{u}_i} = \frac{1}{s^2 + \frac{s}{(RC)} + (1-D)^2\Big/LC} * \left(\frac{1-D}{LC}\right) \qquad (13)$$

V. CLOSED LOOP CONTROL:

The closed loop control consists of inner current loop and outer voltage loop. The inner loop needs a current controller and outer loop requires a voltage controller. The overall block diagram of closed loop control for single phase rectifier is given as follows
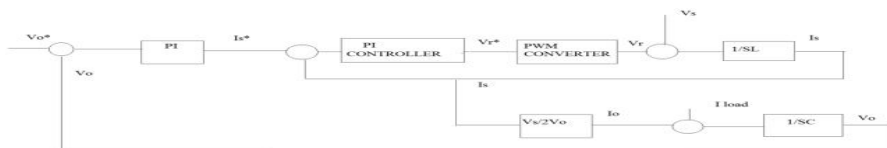

Fig .5. Closed loop block diagram

The comparison of V_{ref} and V_0 produce changes in capacitor voltage, change in capacitor voltage which in turn alter the output current, as output power is equal to input power change in output current will alter the input current. Hence the controller output is given as I_s*(referrence supply current). To match I_s* and I_s it produce fundamental component of

V_r. If I_0 matches I_{load} , no fluctuations in capacitor voltage, but in case not matches means it will produce fluctuations in capacitor voltage and as mentioned above all the parameters alter in order to match the fluctuations.
If we add a product block, multiplying with a sign term which is in phase with V_s, then it will give V_s and I_s in phase with each other, which means UPF in input side.
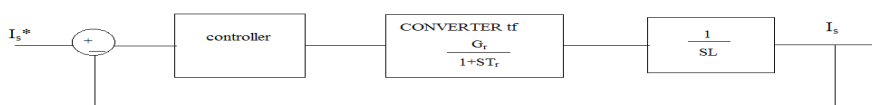
A. INNER CURRENT LOOP CONTROL:

Fig.6. Inner current loop

B. CONVERTER:

$G_r = V_r/M.I$
V_r =Modulating voltage, M.I= Modulating Index
$T_r = 1/f_c$
T_r =Time period, f_c =Carrier Frequency

C. OUTER VOLTAGE LOOP:
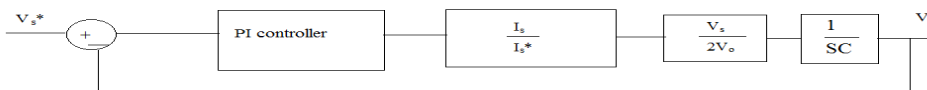
Fig.7. Outer loop

D. CONTROLLER DESIGN:

Input current regulation in the converter is achieved by adjusting the duty cycle. Generally three basic algorithm used are P, PI and PID. Here PI controller in the Inner current loop which regulate the input current, reduce peak over shoot and steady-state error.The PI consists of two basic modes that are proportional modes and integral modes. A proportional controller (k_p) reduced settling time and reduced the error but not eliminated it. An integral controller (k_i) will have the effect of eliminating the steady-state error. Limiter is used to control the duty cycle within the desirable band.

$$k_i = \frac{-D\sin \phi_d}{A_d \sin \beta}$$
$$k_p = \frac{-\sin (-\beta + \phi_d)}{A_d \sin \beta} - \frac{2k_i \cos \beta}{D}$$

$S_d = -\xi\omega_n \pm j\omega_n \sqrt{(1-\xi^2)}$ (Dominant Pole)
ξ = damping ratio
ω_n =natural frequency
$D = |S_d|$
$B = Angle(S_d)$
$A_d = |G\lceil s_d\rceil|$
$\Phi_d = Angle(|G\lceil s_d\rceil|)$

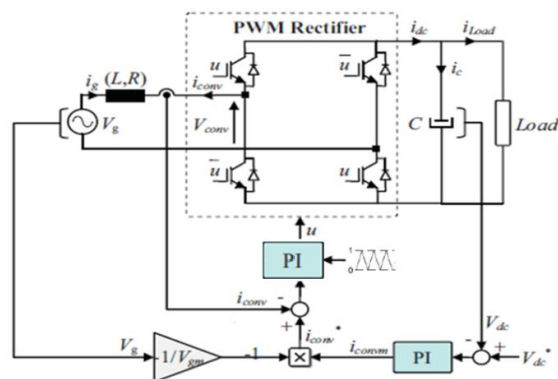The physical model of closed loop control is given as follows

Fig.7.A Closed loop control

E. SIMULATION RESULTS:

Fig.8. shows the inner current loop control and fig.9 shows the outer voltage loop control of a single phase PWM rectifier. Fig.10. shows the combination of inner current loop and outer voltage loop. Fig.11. shows the inner current loop settling for change in reference current. Fig.12. shows the outer current loop settling for different output voltages. Fig.13. the simulated waveform shows the inner current loop settles for different source voltage(V_s). Fig.14. shows the outer voltage loop settles for different load currents. The closed loop control using physical model is simulated with the V_{ref} is given as 400V. The simulation output representing the output voltage settles at 400V is given in the fig.15. and the input current is stabilized using inner current loop which makes input current and voltage in phase,(UPF) is given in the fig.16.
Here the PI controller is designed as K_p=.99724,K_i=53.3. I_{ref}=4A, here after the initial oscillations and peak over shoot, it settles with the given reference value.   For   outer   voltage   loop   the   PI   controller   is   designed   as K_p=.913,K_i=2.27,The V_{ref}=400V.
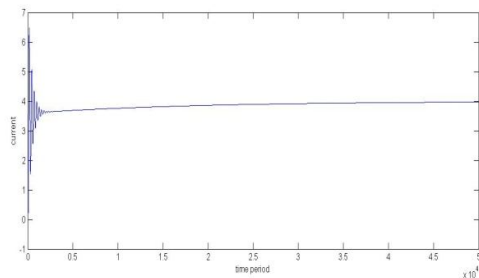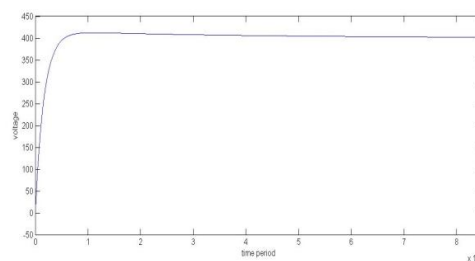

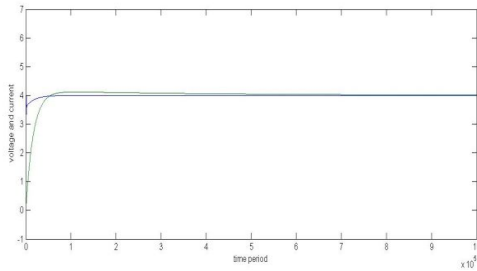Fig.8. Inner Current Loop control

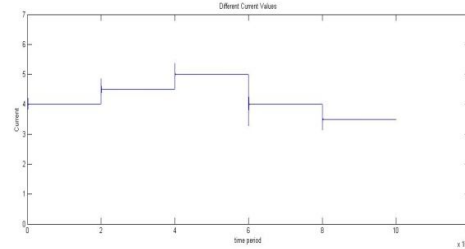

Fig.9. Outer voltage control.
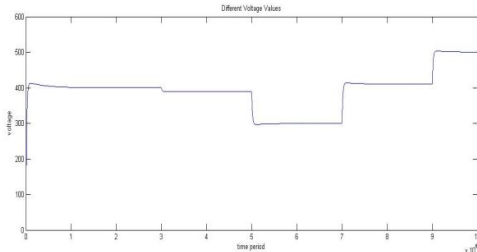
Fig.10. Combined loop

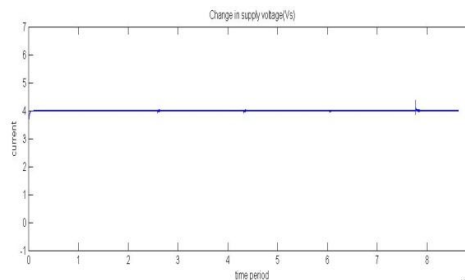Fig.11. Different I_s*

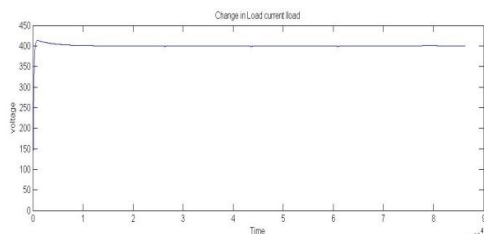Fig.12. Different V_{ref}

Fig.13. Change in V_s(current loop)

Fig.14. Change in Load current I_{load}(voltage loop)

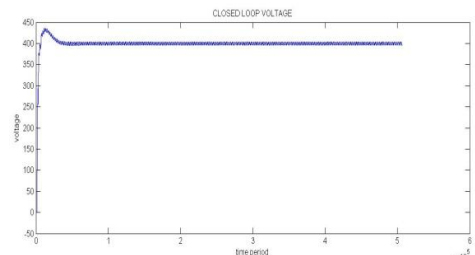Fig.15. Output voltage for closed loop control

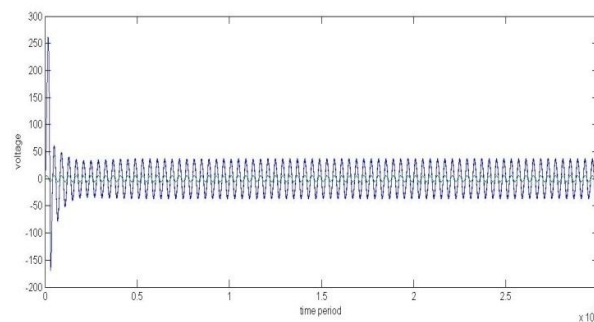Fig.16. Closed Loop Input Voltage and current

VI. SISO MODEL FOR THREE PHASE PWM RECTIFIER

A. INTRODUCTION:

A SISO model is constructed by splitting the *d*-axis and *q*-axis by nonlinear feed forward decoupling and maintaining nearly unity power factor operation. This system is possible to extend the analysis and control design techniques of dc–dc converters to the three-phase PWM rectifier also. The usefulness of the model is demonstrated through closed-loop operation of the rectifier with both voltage mode and inner-current-loop-based schemes.

B. THREE PHASE PWM RECTIFIER:

Over the past several years, considerable research work has been carried out on the control of ac-to-dc Pulse width modulation (PWM) rectifiers, since these converters possess many desirable features such as sinusoidal line currents at a required power factor, a nearly constant dc output voltage, and bidirectional power delivery capability. As the filter capacitor required is generally small under balanced supply voltage conditions, it may also be believed that these converters can offer excellent dynamic response of the dc output voltage.
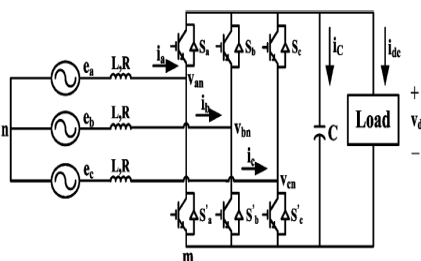

Fig.17.Three Phase PWM Rectifier

Control of three-phase PWM rectifiers in the *d–q* synchronously rotating frame (SRF) has been developed from field oriented control techniques for ac drives in early 1980s. Normally, the control objectives of a PWM rectifier are to regulate the dc output voltage on the dc side, achieve unity power factor (UPF) operation on the ac side, and also to achieve fast dynamic response to line and load disturbances. A state-space averaged model has been proposed for the three-phase PWM rectifier in the *d–q* SRF. However, the model, though accurate, does not give sufficient insight into the controller design and behaviour of the three-phase PWM rectifier system due to its complex multi input–multi output (MIMO) nonlinear structure and the presence of a non minimum phase feature. Due to this, designing a proper controller for such a converter has been generally a challenging task. The SISO model equation has been derived in [1]. It deals with the closed loop control of three phase rectifier with siso model.
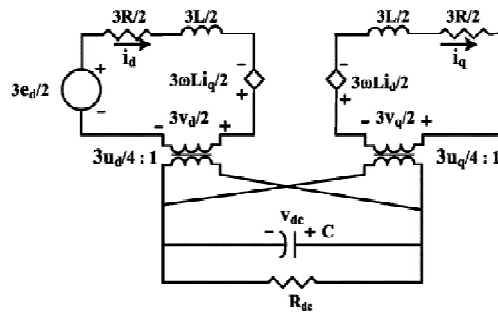

C. EQUIVALENT CIRCUIT FOR SISO MODEL:

Fig.18. Equivalent circuit in SRF

D. NON LINEAR FEEDFORWARD DECOUPLING CONTROLLER:

In Fig.19. the coupling terms between the *d*-axis and the *q*-axis are represented by the two current-controlled dependent voltage sources. Decoupling may be achieved, if the effects of these two voltage sources are nullified by appropriately adjusting the control inputs v_d and v_q
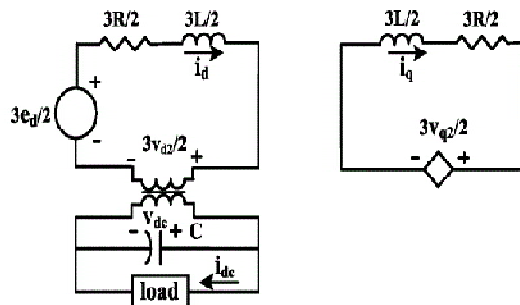

Fig.19. Equivalent circuit in SRF after decoupling q- axis

E. CLOSED LOOP CONTROL:

It is well known that the output performance of a single-phase power factor correction unit is limited by the slow response of the bulky capacitor. This drawback is overcome by a three-phase PWM rectifier as it successfully gets rid of the line-frequency related ripple on the dc side. This allows ripple-free output voltage operation to be achieved even with a small filter capacitor. Here, $Fi(s)$ is the control to- *d*-axis current transfer function given in [1]. In designing a multiloop controller, one first designs the inner loop. Here the controller used is PI controller.   Once   the   current loop is closed, the converter can be treated as a new open-loop plant with transfer function $Fvi(s)$ given in [1].Here this acts as a outer voltage loop model.
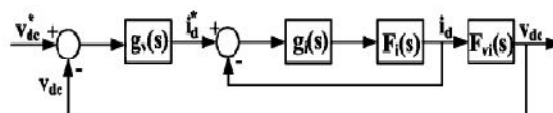

Fig.20. Closed loop control

F. SIMULATION RESULTS:

Fig.21. shows the inner current loop design with a PI controller and Fig.22. shows the outer voltage loop control.

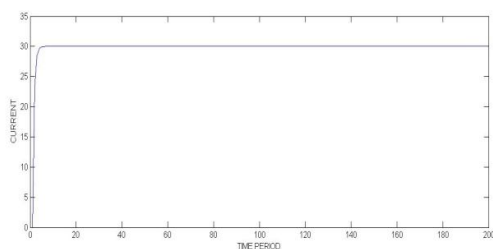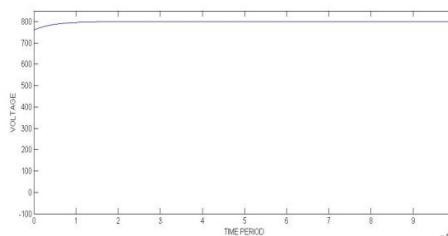

Fig.21.Inner current control

Fig.22. Outer voltage control

Here the closed loop is designed for input voltage E_d=230V, L can be designed as .003H and C=.000136F. The controller used is PI controller and K_p propotional constant is kept unity, while K_i integral constant is designed as 53.3 in Time domain to reduce the steady state error

VII.CONCLUSION

The physical model and mathematical model are designed for single phase rectifier. The closed loop control for single phase PWM rectifier with PI controllers also designed using mathematical model and verified with physical model. SISO model for three phase rectifier and closed loop control are designed for a three phase rectifier. Simulation is done using MATLAB and the simulation results are shown. In future the mathematical SISO model can be simulated.

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